

1. Three propositions are given as

$p$ : It is snowing                       $q$ : The roads are open                       $r$ : We will go skiing

(a) Write the following compound statement in symbolic form.

“It is snowing and the roads are not open.”

(2)

(b) Write the following compound statement in words.

$$(\neg p \wedge q) \Rightarrow r$$

(3)

An incomplete truth table for the compound proposition  $(\neg p \wedge q) \Rightarrow r$  is given below.

(c) Copy and complete the truth table **on your answer paper**.

$p$	$q$	$r$	$\neg p$	$\neg p \wedge q$	$(\neg p \wedge q) \Rightarrow r$
T	T	T			
T	T	F			
T	F	T			
T	F	F			
F	T	T			
F	T	F			
F	F	T			
F	F	F			

(3)

(Total 8 marks)

2. Complete the Truth Table for the compound proposition  $(p \wedge \neg q) \Rightarrow (p \vee q)$ .

$p$	$q$	$\neg q$	$(p \wedge \neg q)$	$(p \vee q)$	$(p \wedge \neg q) \Rightarrow (p \vee q)$
T	T	F	F		
T	F	T	T		
F	T	F		T	
F	F		F	F	

(Total 8 marks)

3. Consider two propositions  $p$  and  $q$ . Complete the truth table below for the compound proposition.

$$(p \wedge \neg q) \Rightarrow (\neg p \vee q)$$

$p$	$q$	$\neg p$	$\neg q$	$p \wedge \neg q$	$\neg p \vee q$	$(p \wedge \neg q) \Rightarrow (\neg p \vee q)$
T	T	F	F	F	<b>(d)</b>	T
T	F	F	T	<b>(b)</b>	F	<b>(f)</b>
F	T	<b>(a)</b>	F	<b>(c)</b>	T	<b>(g)</b>
F	F	T	T	F	<b>(e)</b>	<b>(h)</b>

**(Total 8 marks)**

4. Consider the following statements.

$p$ : students work hard  
 $q$ : students will succeed

- (a) Write the following proposition in symbols using  $p$ ,  $q$  and logical connectives only.

*If students do not work hard, then they will not succeed.*

- (b) Complete the following truth table, relating to the statement made in part (a), and decide whether the statement is logically valid.

$p$	$q$			
T	T			
T	F			
F	T			
F	F			

**(Total 8 marks)**

5. Two propositions  $p$  and  $q$  are defined as follows.

$p$ : Jones passed this course

$q$ : Smith passed this course

(a) Write in symbolic form

(i) *neither Jones nor Smith passed the course;*

(ii) *it is not the case that Jones and Smith both passed the course.*

(b) Complete the following truth table for the logic statement  $\neg p \vee q$ .

$p$	$q$	$\neg p$	$\neg p \vee q$
T	T		
T	F		
F	T		
F	F		

**(Total 4 marks)**