Revision

- 1. A tower can be seen at an angle of α from the level ground. If we move d meters towards the tower, it can be seen at an angle β . Express the height of the tower in terms of d, α and β .
- 2. Let $\triangle ABC$ be a right triangle with the right angle at C. Let D be the foot of the height from C. Let $\angle BAC = \alpha$. Find the angle α if the ratio of the area of the triangle ACD to the area of the triangle ABC is 3:4.
- 3. At what angle can a circle with radius r be seen at a distance of r from the edge of this circle?
- 4. At what distance from centre of the circle with radius 1 will the circle be seen at a right angle?
- 5. In triangle ABC the side AC has been extended by c see picture.



- (a) Show that $2\beta = \alpha$
- (b) Find $\operatorname{tg} \beta$ if $\operatorname{tg} \alpha = \frac{5}{12}$
- (c) Find the exact values of $tg 15^{\circ}$ and $tg 22, 5^{\circ}$.

6. Two right triangles are connected via equal sides as shown below.



- (a) Express x in terms of a, α and β .
- (b) Find the perimeter of the quadrilateral if $a = 2\sqrt{6}$, $\alpha = 30^{\circ}$ and $\beta = 45^{\circ}$.
- 7. In a triangle ABC we have |AB| = 14, |BC| = 9 and $\angle CBA = 60^{\circ}$. Point D lies on the segment BC and |CD| = 8. A circle has been drawn through points C and D and tangent to the segment AB, see diagram below.



Find the radius of the circle.