1. A quadratic function, $f(x) = ax^2 + bx$, is represented by the mapping diagram below.



(a) Use the mapping diagram to write down **two** equations in terms of *a* and *b*.

(2)

- (b) Find the value of
 - (i) *a*;
 - (ii) b. (2)
- (c) Calculate the *x*-coordinate of the vertex of the graph of f(x).

(2) (Total 6 marks) 2. The graph of $y = 2x^2 - rx + q$ is shown for $-5 \le x \le 7$.



The graph cuts the y-axis at (0, 4).

(a) Write down the value of q.

The axis of symmetry is x = 2.5.

- (b) Find the value of *r*.
- (c) Write down the minimum value of *y*.
- (d) Write down the range of *y*.

(2) (Total 6 marks)

(1)

(2)

(1)

3. The following is the graph of the quadratic function y = f(x).



(a) Write down the solutions to the equation f(x) = 0.

(2)

- (b) Write down the equation of the axis of symmetry of the graph of f(x). (2)
- (c) The equation f(x) = 12 has two solutions. One of these solutions is x = 6. Use the symmetry of the graph to find the other solution.

(1)

(d) The minimum value for *y* is -4. Write down the range of f(x).

(1) (Total 6 marks)



4. The graph of a quadratic function y = f(x) is given below.

(2) (Total 6 marks)

(2)

(2)

5. The diagram below shows the graph of a quadratic function. The graph passes through the points (6, 0) and (p, 0). The maximum point has coordinates (0.5, 30.25).



- Calculate the value of *p*. (a)
- Given that the quadratic function has an equation $y = -x^2 + bx + c$ where $b, c \in \mathbb{Z}$, (b) find *b* and *c*. (4)
- A quadratic curve with equation y = ax(x b) is shown in the following diagram. 6.

- The x-intercepts are at (0, 0) and (6, 0), and the vertex V is at (h, 8).
- Find the value of *h*. (a)
- (b) Find the equation of the curve.

Factorise the expression $x^2 - kx$. 7. (a)



- (4) (Total 6 marks)
 - (1)

(2)

(2)

(Total 6 marks)

5

(b) Hence solve the equation $x^2 - kx = 0$.

(1)

The diagram below shows the graph of the function $f(x) = x^2 - kx$ for a particular value of k.



(c) Write down the value of *k* for this function.

(1)

(d) Find the minimum value of the function y = f(x).

(3) (Total 6 marks)

- 8. The graph of a quadratic function f(x) intersects the horizontal axis at (1, 0) and the equation of the axis of symmetry is x = -1.
 - (a) Write down the *x*-coordinate of the other point where the graph of y = f(x) intersects the horizontal axis.
 - (b) y = f(x) reaches its maximum value at y = 5.
 - (i) Write down the value of f(-1).
 - (ii) Find the range of the function y = f(x).

(Total 6 marks)

- 9. (a) Sketch the graph of the function $y = 2x^2 6x + 5$.
 - (b) Write down the coordinates of the local maximum or minimum of the function.
 - (c) Find the equation of the axis of symmetry of the function.

(Total 6 marks)

10. The diagram below shows the graph of $y = c + kx - x^2$, where k and c are constants.



- (a) Find the values of k and c.
- (b) Find the coordinates of Q, the highest point on the graph.

(Total 8 marks)