

Self-assessment: 9 Circular measure and trigonometric functions

1. Find the constants *a*, *b*, *c*, *d* in the equations of the two graphs below:





(accessible to students on the path to grade 5 or 6) [7 marks]

2. Find the exact period of the function $f(x) = \sin 4x + \sin 6x$.

(accessible to students on the path to grade 3 or 4) [3 marks]



3. The depth of water in a harbour varies with time as $h = 8.6 + 1.2 \sin\left(\frac{\pi t}{6}\right)$, where *h* is the depth measured in metres and *t* is time in hours after midnight.

- (a) Find the depth of the water at 2 p.m.
- (b) What is the least depth of the water?
- (c) At what times is the depth of the water 8.1 m?
- (d) A ship can enter the harbour when the water depth is above 9 m. Find the times when the ship can enter the harbour.

(accessible to students on the path to grade 3 or 4) [8 marks]

4. Do not use a calculator to answer this question.

Let
$$f(x) = 3 \sin\left(x + \frac{\pi}{4}\right)$$
 for $x \in [0, 2\pi]$.

(a) Find the exact value of
$$f\left(\frac{\pi}{12}\right)$$
.

(accessible to students on the path to grade 5 or 6)

- (b) Find the exact values of all the zeroes of f.
- (c) State the minimum value of 5 f(x).

Another function is defined by
$$g(x) = \tan\left(x - \frac{\pi}{4}\right)$$
 for $x \in [0, 2\pi]$.

(accessible to students on the path to grade 3 or 4)

(d) Find the exact value of
$$g\left(\frac{\pi}{2}\right)$$
.

(e) By sketching graphs, or otherwise, find the number of solutions of the equation f(x) = g(x).

(accessible to students on the path to grade 5 or 6)

[12 marks]