1. Consider the two propositions *p* and *q*.

*p*: The sun is shining *q*: I will go swimming

Write in words the compound propositions

(a) 
$$p \Rightarrow q;$$
 (2)

(b) 
$$\neg p \lor q$$
. (2)

The truth table for these compound propositions is given below.

| р | q | $p \Rightarrow q$ | $\neg p$ | $\neg p \lor q$ |
|---|---|-------------------|----------|-----------------|
| Т | Т | Т                 |          | Т               |
| Т | F | F                 |          | F               |
| F | Т | Т                 |          | Т               |
| F | F | Т                 |          | Т               |

(c) Complete the column for  $\neg p$ .

(d) State the relationship between the compound propositions  $p \Rightarrow q$  and  $\neg p \lor q$ .

(1) (Total 6 marks)

(1)

2. Two logic propositions are given

*p: Dany goes to the cinema q: Dany studies for the test* 

(a) Write in words the proposition

 $p \underline{\vee} q.$ 

- (b) Given the statement s: "If Dany goes to the cinema then Dany doesn't study for the test".
  - (i) Write *s* in symbolic form.
  - (ii) Write in symbolic form the contrapositive of part (b)(i).

(Total 6 marks)

- **3.** Consider the following statements:
  - p: Good mathematics students go to good universities
  - q: Good music students are good mathematics students
  - r: Students who go to good universities get good jobs
  - (a) From these statements, write two **valid** conclusions.
  - (b) Write in words each of the following
    - (i)  $\neg q$ ;
    - (ii)  $p \wedge r$ .

(Total 4 marks)

- 4. Three propositions are given as
  - p: It is snowing q: The roads are open r: We will go skiing
  - (a) Write the following compound statement in symbolic form.

"It is snowing and the roads are not open."

(2)

(3)

(b) Write the following compound statement in words.

$$(\neg p \land q) \Rightarrow r$$

An incomplete truth table for the compound proposition  $(\neg p \land q) \Rightarrow r$  is given below.

(c) Copy and complete the truth table **on your answer paper**.

| р | q | r | $\neg p$ | $\neg p \land q$ | $(\neg p \land q) \Rightarrow r$ |
|---|---|---|----------|------------------|----------------------------------|
| Т | Т | Т |          |                  |                                  |
| Т | Т | F |          |                  |                                  |
| Т | F | Т |          |                  |                                  |
| Т | F | F |          |                  |                                  |
| F | Т | Т |          |                  |                                  |
| F | Т | F |          |                  |                                  |
| F | F | Т |          |                  |                                  |
| F | F | F |          |                  |                                  |

(3) (Total 8 marks) 5. Consider each of the following statements:

*p*: Alex is from Uruguay*q*: Alex is a scientist*r*: Alex plays the flute

- (a) Write each of the following arguments in symbols:
  - (i) If Alex is not a scientist then he is not from Uruguay.
  - (ii) If Alex is a scientist, then he is either from Uruguay or plays the flute.

(3)

(b) Write the following argument in words:

$$\neg r \Rightarrow \neg (q \lor p)$$

(3)

(c) Construct a truth table for the argument in part (b) using the values below for p, q, r and  $\neg r$ . Test whether or not the argument is logically valid.

| р | q | r | $\neg r$ |
|---|---|---|----------|
| Т | Т | Т | F        |
| Т | Т | F | Т        |
| Т | F | Т | F        |
| Т | F | F | Т        |
| F | Т | Т | F        |
| F | Т | F | Т        |
| F | F | Т | F        |
| F | F | F | Т        |

(4) (Total 10 marks) 6. Let  $\mathscr{C} = \{x : 1 \le x < 17, x \in \mathbb{N}\}.$ 

P , Q and R are the subsets of  $\,\%\,$  such that

 $P = \{ \text{multiples of four} \};$  $Q = \{ \text{factors of 36} \};$  $R = \{ \text{square numbers} \}.$ 

- (a) List the elements of
  - (i) E

(ii)

- $P \cap Q \cap R.$  (2)
- (b) Describe in words the set  $P \cup Q$ .
- (c) (i) Draw a Venn diagram to show the relationship between sets P, Q and R. (2)
  - (ii) Write the elements of  $\mathscr{C}$  in the appropriate places on the Venn diagram. (3)
- (d) Let p, q and r be the statements

*p*: *x* is a multiple of four;

- *q*: *x* is a factor of 36;
- *r*: *x* is a square number.
- (i) Write a sentence, in words, for the statement

$$(p \lor r) \land \neg q \tag{2}$$

- (ii) Shade the region on your Venn diagram in part (c)(i) that represents  $(p \lor r) \land \neg q$
- (iii) (a) Use a truth table to determine the values of  $(p \lor r) \land \neg q$ . Write the first three columns of your truth table in the following format.

| р | q | r |
|---|---|---|
| Т | Т | Т |
| Т | Т | F |
| Т | F | Т |
| Т | F | F |
| F | Т | Т |
| F | Т | F |
| F | F | Т |
| F | F | F |

(3)

(1)

(1)

(b) Write down one possible value of x for which  $(p \lor r) \land \neg q$  is true.

(1) (Total 15 marks)