Self-assessment: 2 Exponents and logarithms

Stratidge Resource

1. Do not use a calculator to answer this question.

- (a) Find the exact value of $3 \log(5) \log(20) + \log(16)$.
- (b) Given that $x = \ln 2$, $y = \ln 3$ and $z = \ln 5$, express $\ln\left(\frac{45}{4}\right)$ in terms of x, y and z.
- (c) If $\ln K = 2 \ln c$, find and simplify an expression for *K* in terms of *c*.

(accessible to students on the path to grade 3 or 4) [6 marks]

2. Do not use a calculator to answer this question.

Solve the following equation:

$$\log_2(x+2) - \log_2 x = 3$$

(accessible to students on the path to grade 3 or 4) [3 marks]

3. Find the exact solutions of the equation,

$$3e^{2x} - 7e^x + 2 = 0$$

(accessible to students on the path to grade 5 or 6) [5 marks]

4. The diagram shows the graph with equation $y = C + Ae^{-kt}$. The graph passes through the point P(2, 3).





- (a) Write down the value of *C* and the value of *A*.
- (b) Find the exact value of *k*.

(accessible to students on the path to grade 5 or 6) [5 marks]

- 5. (a) The population of bacteria increases according to an exponential model, $N = A \times b^{kt}$, where N is the number of bacteria after t minutes and A and b are positive constants. Given that initially there were 50 bacteria and that after three minutes the number has grown to 270,
 - (i) Write down the value of A.
 - (ii) Show that, to three significant figures, $b^k = 1.75$.
 - (iii) Find the size of the population after five minutes.
 - (b) After five minutes the population growth slows down, so that now it follows the new model,

$$N = 2000 - M e^{-0.47t}.$$

- (i) Find the value of *M*.
- (ii) According to this model, the size of the population approaches a limit in the long term. Find this limit.
- (iii) How long does it take for the population size to reach1999? Give your answer to the nearest minute.

(accessible to students on the path to grade 5 or 6) [11 marks]