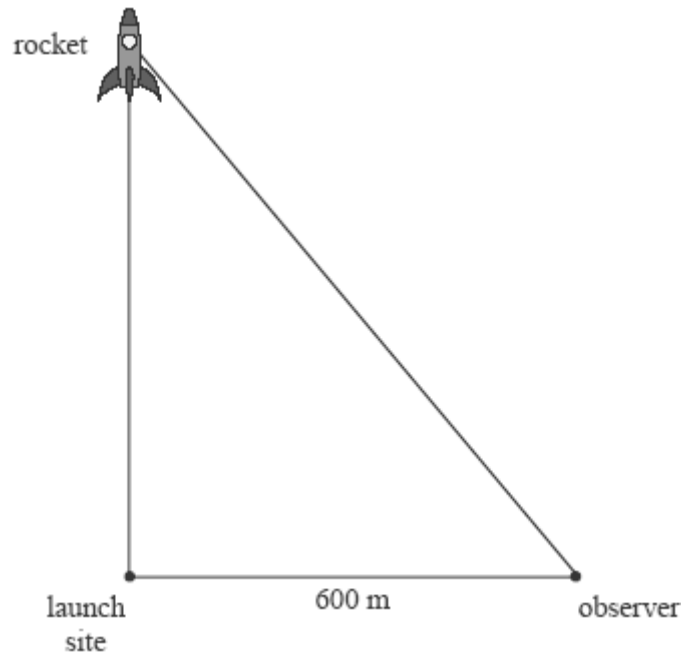
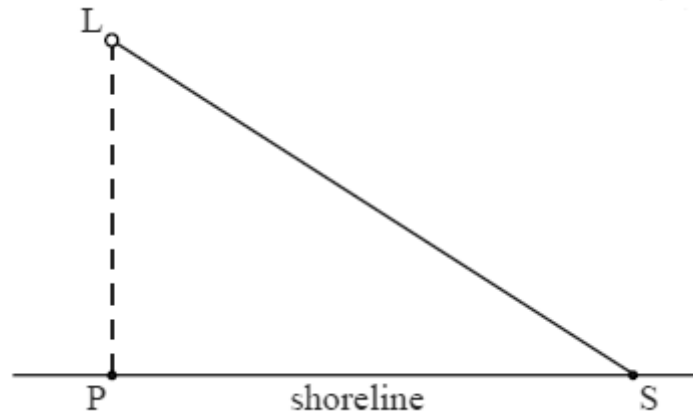


1. A rocket is rising vertically at a speed of  $300 \text{ m s}^{-1}$  when it is  $800 \text{ m}$  directly above the launch site. Calculate the rate of change of the distance between the rocket and an observer, who is  $600 \text{ m}$  from the launch site and on the same horizontal level as the launch site.



*diagram not to scale*  
(Total 6 marks)

2. A lighthouse  $L$  is located offshore, 500 metres from the nearest point  $P$  on a long straight shoreline. The narrow beam of light from the lighthouse rotates at a constant rate of  $8\pi$  radians per minute, producing an illuminated spot  $S$  that moves along the shoreline. You may assume that the height of the lighthouse can be ignored and that the beam of light lies in the horizontal plane defined by sea level.



When  $S$  is 2000 metres from  $P$ ,

- (a) show that the speed of  $S$ , correct to three significant figures, is 214 000 metres per minute;

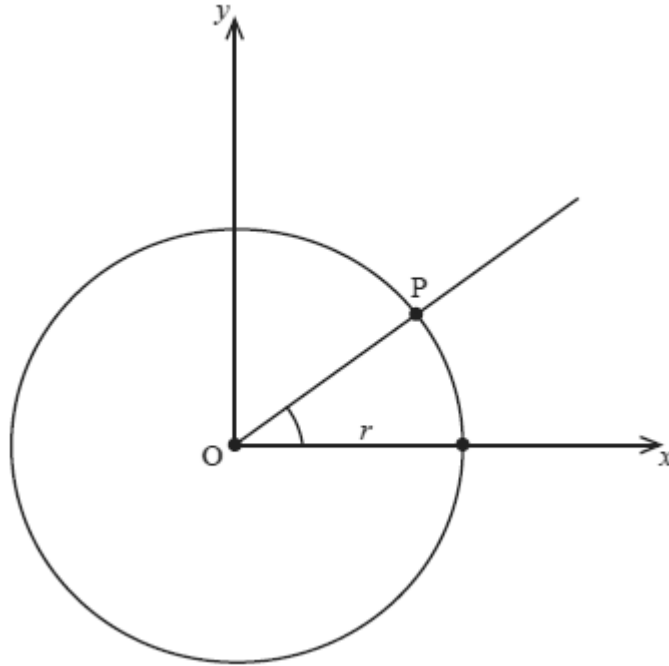
(5)

- (b) find the acceleration of  $S$ .

(3)

(Total 8 marks)

3. The diagram below shows a circle with centre at the origin  $O$  and radius  $r > 0$ .



A point  $P(x, y)$ , ( $x > 0, y > 0$ ) is moving round the circumference of the circle.

Let  $m = \tan\left(\arcsin\frac{y}{r}\right)$ .

(a) Given that  $\frac{dy}{dt} = 0.001r$ , show that  $\frac{dm}{dt} = \left(\frac{r}{10\sqrt{r^2 - y^2}}\right)^3$ .

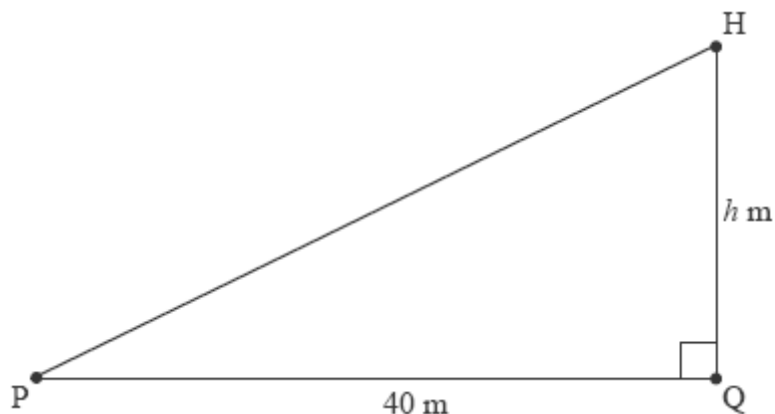
(6)

(b) State the geometrical meaning of  $\frac{dm}{dt}$ .

(1)

(Total 7 marks)

4. A helicopter H is moving vertically upwards with a speed of  $10 \text{ m s}^{-1}$ . The helicopter is  $h \text{ m}$  directly above the point Q, which is situated on level ground. The helicopter is observed from the point P, which is also at ground level, and  $PQ = 40 \text{ m}$ . This information is represented in the diagram below.



*diagram not to scale*

When  $h = 30$ ,

- (a) show that the rate of change of  $\widehat{HPQ}$  is  $0.16$  radians per second;

(3)

- (b) find the rate of change of PH.

(4)

(Total 7 marks)