

1. Consider the universal set  $U = \{x \in \mathbb{N} \mid 3 < x < 13\}$ , and the subsets  $A = \{\text{multiples of } 3\}$  and  $B = \{4, 6, 12\}$ .

(a) List the elements of the following sets.

(i)  $A$

(ii)  $A \cap B'$

(2)

(b) Write down one element of  $(A \cup B)'$ .

(2)

(c) One of the statements in the table below is false. Indicate with an **X** which statement is false. Give a reason for your answer.

$n(A \cup B) = 4$	
$15 \in A'$	
$A \subset A \cup B$	

(2)

(Total 6 marks)

2. The universal set  $U$  is the set of integers from 1 to 20 inclusive.

$A$  and  $B$  are subsets of  $U$  where:

$A$  is the set of even numbers between 7 and 17.

$B$  is the set of multiples of 3.

List the elements of the following sets:

(a)  $A$ ;

(1)

(b)  $B$ ;

(1)

(c)  $A \cup B$ ;

(2)

(d)  $A \cap B'$ .

(2)

(Total 6 marks)

3. Let  $U = \{-4, -\frac{2}{3}, 1, \pi, 13, 26.7, 69, 10^{33}\}$ .

$A$  is the set of all the integers in  $U$ .

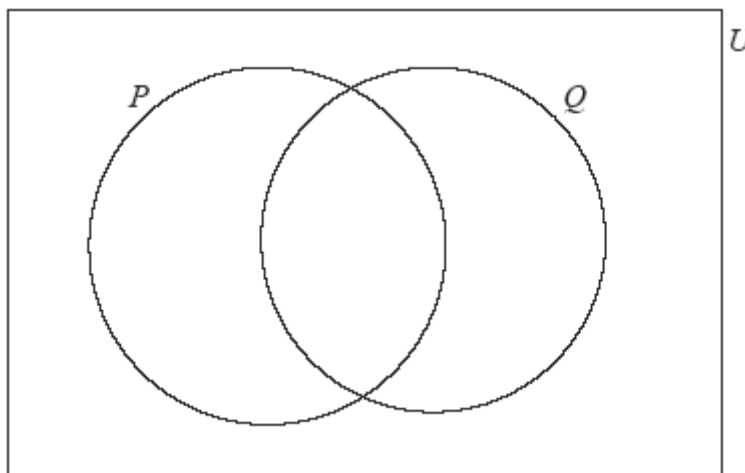
$B$  is the set of all the rational numbers in  $U$ .

- (a) List all the prime numbers contained in  $U$ .
- (b) List all the members of  $A$ .
- (c) List all the members of  $B$ .
- (d) List all the members of the set  $A \cap B$ .

(Total 8 marks)

4. The sets  $P$ ,  $Q$  and  $U$  are defined as

$U = \{\text{Real Numbers}\}$ ,  $P = \{\text{Positive Numbers}\}$  and  $Q = \{\text{Rational Numbers}\}$ .



Write down in the correct region on the Venn diagram the numbers

$\frac{22}{7}$ ,  $5 \times 10^{-2}$ ,  $\sin(60^\circ)$ ,  $0$ ,  $\sqrt[3]{-8}$ ,  $-\pi$

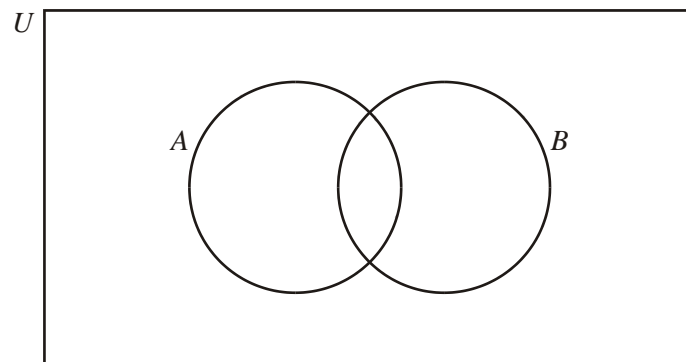
(Total 6 marks)

5. The universal set  $U$  is defined as the set of positive integers less than 10. The subsets  $A$  and  $B$  are defined as:

$$A = \{\text{integers that are multiples of 3}\}$$

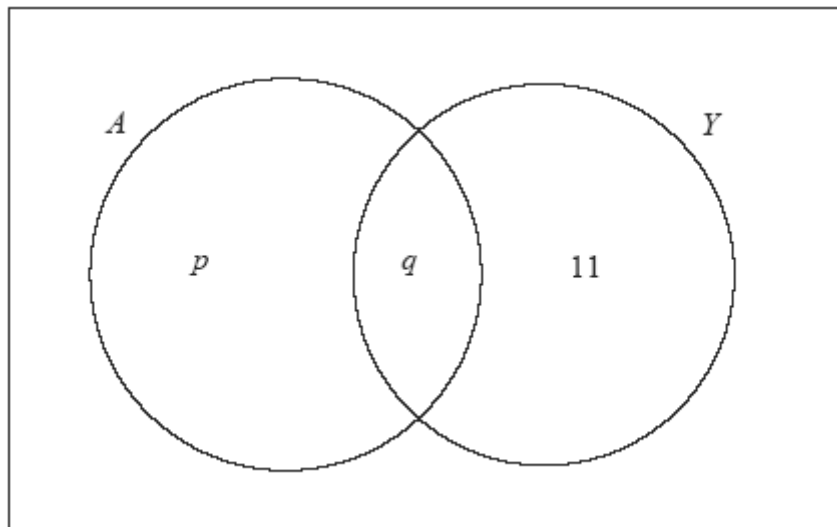
$$B = \{\text{integers that are factors of 30}\}$$

- (a) List the elements of
- (i)  $A$ ;
  - (ii)  $B$ .
- (b) Place the elements of  $A$  and  $B$  in the appropriate region in the Venn diagram below.



**(Total 4 marks)**

6. A fitness club has 60 members. 35 of the members attend the club's aerobics course ( $A$ ) and 28 members attend the club's yoga course ( $Y$ ). 17 members attend both courses. A Venn diagram is used to illustrate this situation.



- (a) Write down the value of  $q$ . (1)
- (b) Find the value of  $p$ . (2)
- (c) Calculate the number of members of the fitness club who attend neither the aerobics course ( $A$ ) nor the yoga course ( $Y$ ). (2)
- (d) Shade, on your Venn diagram,  $A' \cap Y$ . (1)

(Total 6 marks)