Batory preIB

Name: Group 1 Result:

- 1. (1 point) Let $X = \{1, 2, 3, 4, 5\}$ and $Y = \{4, 5, 6, 7\}$. Select all true statements:
 - A. $2 \in X \cap Y$ B. $2 \in X Y$ C. $2 \in Y X$ D. $2 \in X \cup Y$
- 2. (1 point) In a group of 20 students, 7 have blond hair and 8 have blue eyes. 9 students have neither blond hair nor blue eyes. How many students have blond hair but do **not** have blue eyes?

A. 3 B. 4 C. 6 7

3. (1 point)
$$\left(\frac{1}{12}\right)^{-\frac{1}{2}} = (\text{select all that apply})$$

A. $\sqrt{12}$ B. $\sqrt{18} - \sqrt{6}$ C. $\sqrt{75} - \sqrt{27}$ D. $\frac{\sqrt{6}}{\sqrt{2}}$

4. (1 point) Let $U = \mathbb{R}$, $X =] - \infty$, 1] and Y =]1, 2[. Which of the following statements are true? Select all that apply.

A.
$$X \cap Y = \emptyset$$

B. $X - Y = X$
C. $(X \cup Y)' =]2, \infty[$
D. $X \cup Y =]-\infty, 2[$

- 5. (1 point) How many **positive integers** satisfy the inequality 15 5x > 4 2x?
 - A. 3 B. 4 C. 5 D. infinitely many

6. (2 points) Prove that the number $3^{999} + 3^{997}$ is divisible by 30.

7. (3 points) Prove that $\sqrt{6}$ is an irrational number.

8. (3 points) Find the set of values of x that satisfy the following system of inequalities:

$$\begin{cases} \frac{7-x}{2} > x - 1\\ \frac{x-2}{2} - x \leqslant \frac{x-1}{4} \end{cases}$$

Represent the solution on the number line and list all integers that satisfy both inequalities.

9. (2 points) Write the following in the form 3^k where $k \in \mathbb{Q}$

$$\frac{\sqrt{3} \times \frac{1}{9} \times 81^2}{(3\sqrt[3]{3})^4}$$

10. (5 points) There are 30 students in a year. Let F be the set of students who take Further Mathematics class, M the set of students who take the Mathematics class and P the set of students who take Physics class.

Every student who takes Further Mathematics also takes Mathematics. 3 students take Further Mathematics and Physics.

2 students who take Further Mathematics do not take Physics.

- 10 students in total take both Mathematics and Physics.
- 12 students take Physics.
- 22 students take Mathematics.
- (a) Draw a Venn diagram to represent the above information.
- (b) How many students:
 - i. do not take Further Mathematics?
 - ii. take Physics only?
 - iii. do not take any of the three mentioned subjects?
- (c) On your diagram shade the region corresponding to the set $M \cap (F \cup P)'$.