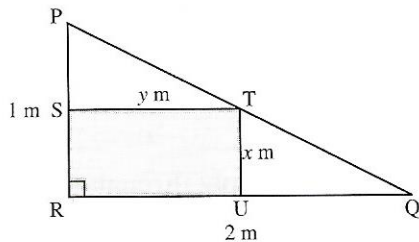


- 7 When a stone is projected vertically into the air with an initial speed of  $30 \text{ m s}^{-1}$  its height,  $h$  metres, above the point of projection, at a time  $t$  seconds after the instant of projection, can be approximated by the formula  $h = 30t - 5t^2$ .
- Find the maximum height reached by the stone, and the time at which this occurs.
- 8 A strip of wire of length 28 cm is cut into two pieces. One piece is bent to form a square of side  $x$  cm, and the other piece is bent to form a rectangle of width 3 cm.
- Show that the lengths of the other two sides of the rectangle are given by  $(11 - 2x)$  cm.
  - Deduce that the total combined area of the square and the rectangle is  $(x^2 - 6x + 33) \text{ cm}^2$ .
  - Prove that the minimum total area which can be enclosed in this way is  $24 \text{ cm}^2$ .
- 9 A string of length 60 cm is cut into two pieces and each piece is formed into a rectangle. The first rectangle has width 6 cm, and the second rectangle is three times as long as it is wide. Given the width of the second rectangle is  $x$  cm,
- deduce that the total combined area enclosed by the two rectangles may be expressed as  $[3(x - 4)^2 + 96] \text{ cm}^2$
  - show that the minimum area which can be enclosed in this way is  $96 \text{ cm}^2$ .

- 10 It is required to fit a rectangle of maximum area inside a triangle, PQR, in which  $PR = 1$  metre,  $RQ = 2$  metres, and  $\angle PRQ = 90^\circ$ . The diagram shows an arbitrary rectangle, RSTU, in which  $TU = x$  metres and  $ST = y$  metres.



- Show that  $y = 2 - 2x$ .
  - Find an expression, in terms of  $x$ , for the area of the rectangle, and deduce that the rectangle of maximum area which fits inside triangle PQR has area  $\frac{1}{2} \text{ m}^2$ .
- \*11 Show that, in general, for any rectangle drawn inside any right-angled triangle, the area of the rectangle cannot exceed half the area of the triangle.