

- (a) evidence of addition (M1)
e.g. at least two correct elements
- $$A + B = \begin{pmatrix} 4 & 2 \\ 1 & 0 \end{pmatrix} \quad \text{A1 N2}$$
- (b) evidence of multiplication (M1)
e.g. at least two correct elements
- $$-3A = \begin{pmatrix} -3 & -6 \\ -9 & 3 \end{pmatrix} \quad \text{A1 N2}$$
- (c) evidence of matrix multiplication (in correct order) (M1)
e.g. $AB = \begin{pmatrix} 1(3)+2(-2) & 1(0)+2(1) \\ 3(3)+(-1)(-2) & 3(0)+(-1)(1) \end{pmatrix}$
- $$AB = \begin{pmatrix} -1 & 2 \\ 11 & -1 \end{pmatrix} \quad \text{A2 N3}$$

[7]

- (a) $\det A = 2$ (A1)
- $$A^{-1} = \frac{1}{2} \begin{pmatrix} 3 & 4 \\ 1 & 2 \end{pmatrix} \left(= \begin{pmatrix} \frac{3}{2} & 2 \\ \frac{1}{2} & 1 \end{pmatrix} \right) \quad \text{A1 N2 2}$$
- (b) evidence of multiplying by A^{-1} (M1)
- e.g.* $X = A^{-1} \begin{pmatrix} 4 & 6 \\ 2 & -2 \end{pmatrix}, A^{-1}B$
- correct working A1
- $$\text{e.g. } X = \frac{1}{2} \begin{pmatrix} 3 & 4 \\ 1 & 2 \end{pmatrix} \begin{pmatrix} 4 & 6 \\ 2 & -2 \end{pmatrix} \begin{pmatrix} \frac{3}{2} & 2 \\ \frac{1}{2} & 1 \end{pmatrix} \begin{pmatrix} 4 & 6 \\ 2 & -2 \end{pmatrix} \frac{1}{2} \begin{pmatrix} 20 & 10 \\ 8 & 2 \end{pmatrix}$$
- $$X = \begin{pmatrix} 10 & 5 \\ 4 & 1 \end{pmatrix} \quad \text{A2 N3 4}$$

[6]

(a) evidence of considering determinant (M1)

e.g. $3 \times -3 - (-2) \times x$, attempt to find inverse

setting the determinant equal to zero (M1)

e.g. $-9 + 2x = 0$, $2x = 9$

$$x = \frac{9}{2}$$

A1 N2 3

(b) **METHOD 1**

$$\mathbf{A}^{-1} = \frac{1}{-9+2x} \begin{pmatrix} -3 & -x \\ 2 & 3 \end{pmatrix} \quad (\text{A1}) \quad (\text{A1})$$

Note: Award A1 for $\frac{1}{\det \mathbf{A}}$, A1 for $\begin{pmatrix} -3 & -x \\ 2 & 3 \end{pmatrix}$.

one correct equation from $\mathbf{A} = \mathbf{A}^{-1}$ (A1)

$$\text{e.g. } \frac{-3}{-9+2x} = 3, \frac{2}{-9+2x} = 2, \frac{3}{-9+2x} = -3, \frac{-x}{-9+2x} = x$$

attempt to solve the equation (M1)

e.g. $-3 = 3(-9 + 2x)$, $-9 + 2x = -1$

$x = 4$ (do not accept $x = 4$, $x = 0$) A1 N4 5

METHOD 2

$$\mathbf{A}^2 = \mathbf{I} \quad (\text{A1})$$

$$\mathbf{A}^2 = \begin{pmatrix} 9-2x & 0 \\ 0 & -2x+9 \end{pmatrix} \quad (\text{A1})$$

one correct equation from $\mathbf{A}^2 = \mathbf{I}$ (A1)

e.g. $9 - 2x = 1$

attempt to solve the equation (M1)

e.g. $2x = 8$

$x = 4$ A1 N4 5

[8]

- (a) evidence of multiplying
e.g. one correct element (M1)

$$AB = \begin{pmatrix} -15 \\ 5 \end{pmatrix} \quad A1A1 \quad N3$$

(b) METHOD 1

evidence of multiplying by A (on left or right) (M1)

$$\text{e.g. } AA^{-1} X = AB, X = AB$$

$$X = \begin{pmatrix} -15 \\ 5 \end{pmatrix} \text{ (accept } x = -15, y = 5\text{)} \quad A1 \quad N2$$

METHOD 2

attempt to set up a system of equations (M1)

$$\text{e.g. } \frac{4x+2y}{10} = -5, \frac{-3x+y}{10} = 5$$

$$X = \begin{pmatrix} -15 \\ 5 \end{pmatrix} \text{ (accept } x = -15, y = 5\text{)} \quad A1 \quad N2$$

[5]

$$(a) (i) AB = \begin{pmatrix} 4 & 0 \\ 0 & 4 \end{pmatrix} (= 4I) \quad A2 \quad N2$$

$$(ii) A^{-1} = \frac{1}{4} \begin{pmatrix} 2 & -1 \\ -6 & 5 \end{pmatrix} \frac{1}{4} B, \begin{pmatrix} \frac{1}{2} & -\frac{1}{4} \\ \frac{3}{2} & \frac{5}{4} \end{pmatrix} \quad A1 \quad N1$$

(b) METHOD 1

$$\begin{pmatrix} x \\ y \end{pmatrix} = A^{-1} C \quad (M1)$$

$$= \frac{1}{4} \begin{pmatrix} 2 & -1 \\ -6 & 5 \end{pmatrix} \begin{pmatrix} 8 \\ -4 \end{pmatrix} \left(\begin{pmatrix} \frac{1}{2} & -\frac{1}{4} \\ \frac{3}{2} & \frac{5}{4} \end{pmatrix} \begin{pmatrix} 8 \\ -4 \end{pmatrix} \right) \quad A1$$

$$\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 5 \\ -17 \end{pmatrix} \quad A1A1 \quad N3$$

METHOD 2

$$5x + y = 8, 6x + 2y = -4 \quad A1 \\ \text{for work towards solving their system} \quad (M1)$$

$$\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 5 \\ -17 \end{pmatrix} \quad A1A1 \quad N3$$

[7]

(a) **METHOD 1**

$$\mathbf{M} = (\mathbf{M}^{-1})^{-1} \quad (\text{M1})$$

$$\mathbf{M} = \frac{1}{10} \begin{pmatrix} 2 & 0 \\ -1 & 5 \end{pmatrix} \quad \text{A1A1 N3}$$

METHOD 2

$$\begin{pmatrix} a & b \\ c & d \end{pmatrix} \begin{pmatrix} 5 & 0 \\ 1 & 2 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \quad (\text{M1})$$

$$5a + b = 1, 2b = 0, 5c + d = 0, 2d = 1 \quad (\text{A1})$$

$$\mathbf{M} = \begin{pmatrix} 0.2 & 0 \\ -0.1 & 0.5 \end{pmatrix} \quad \text{A1 N3}$$

(b) **METHOD 1**

evidence of appropriate approach (M1)

e.g. $\mathbf{X} = \mathbf{M}^{-1} \mathbf{B}$

$$\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 5 & 0 \\ 1 & 2 \end{pmatrix} \begin{pmatrix} 1 \\ 7 \end{pmatrix} \quad \text{A1}$$

$$= \begin{pmatrix} 5 \\ 15 \end{pmatrix} \quad \text{A1 N2}$$

METHOD 2

evidence of appropriate approach (M1)

e.g. $\begin{pmatrix} 0.2 & 0 \\ -0.1 & 0.5 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 1 \\ 7 \end{pmatrix}$

$$0.2x = 1, -0.1x + 0.5y = 7 \quad \text{A1}$$

$$\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 5 \\ 15 \end{pmatrix} \quad \text{A1 N2}$$

[6]

(a) evidence of correct method (M1)
e.g. at least 1 correct element (must be in a 2×2 matrix)

$$AB = \begin{pmatrix} -2 - 2q & 0 \\ -6 + pq & 3 + \frac{p}{2} \end{pmatrix}$$

A1 N2

(b) **METHOD 1**
evidence of using $AB = I$ (M1)
2 correct equations A1A1
e.g. $-2 - 2q = 1$ and $3 + \frac{p}{2} = 1$, $-6 + pq = 0$

$$p = -4, q = -\frac{3}{2}$$

A1A1 N1N1

METHOD 2

finding $A^{-1} = \frac{1}{p+6} \begin{pmatrix} p & 2 \\ -3 & 1 \end{pmatrix}$ A1

evidence of using $A^{-1} = B$ (M2)

$$\text{i.e. } \frac{2}{p+6} = 1 \text{ and } -\frac{3}{p+6} = q, \frac{p}{p+6} = -2 \text{ and } -\frac{3}{p+6} = q$$

$$p = -4, q = -\frac{3}{2}$$

A1A1 N1N1

[7]

(a) Attempt to multiply *e.g.* $\begin{pmatrix} 1+0 & -2-6 \\ 0+0 & 0+9 \end{pmatrix}$ (M1)

$$A^2 = \begin{pmatrix} 1 & -8 \\ 0 & 9 \end{pmatrix}$$

A1 N2

(b) $3X + \begin{pmatrix} 1 & -2 \\ 0 & 3 \end{pmatrix} = \begin{pmatrix} -3 & 4 \\ 2 & 1 \end{pmatrix}$ (M1)

$$3X = \begin{pmatrix} -4 & 6 \\ 2 & -2 \end{pmatrix}$$

(A1)

$$X = \frac{1}{3} \begin{pmatrix} -4 & 6 \\ 2 & -2 \end{pmatrix}$$

A1 N2

[5]