

Name:

Group A

Result:

**1.**

[7 points]

Solve for  $x$ :

a)  $\log_9(x - 2) = -\frac{1}{2}$

b)  $16^{x+1} = \left(\frac{1}{2\sqrt{2}}\right)^{2x-4}$

c)  $\log_2(x - 4) - \log_2(x + 1) = -1$

d)  $3^{2x+1} + 5 \cdot 3^x = 2$

e)  $\log_2 x + \log_2(x - 2) = 3$

**2.**

[3 points]

If  $\log_3 2 = P$  and  $\log_3 5 = Q$ , write in terms of  $P$  and  $Q$ :

a)  $\log_3 20 =$

b)  $\log_3 0.08 =$

c)  $\log_3 90 =$

**3.**

[2 points]

Tomasz invests 5000PLN into an account that pays 6% per annum compounded quarterly.

a) Find the value of his investment after 6 years.

b) How many quarter will it take for the investment to double in value?

**4.**

[2 points]

Population of a certain town in  $t$  years after 2021 is given by the formula:

$$P(t) = 16000 \cdot (1.07)^t$$

a) The population increases by  $p\%$  each year. State the value of  $p$ .

b) In which year will the population reach 30000?

**5.***[3 points]*

The value of a certain car decreases by 12% each year. The car is now valued at 65 000 PLN.

- a) Estimate the value of the car in 5 years.
- b) How long will it take for the value to drop below 10 000 PLN?

**6.***[3 points]*

Radium-204 has a half life of 4 milliseconds. Starting with 2 grams of Radium-204:

- a) How much will be left after 4 milliseconds?
- b) How much will be left after 8 milliseconds?
- c) How long will it take for the amount of radium to decay by 10%.