

# Markscheme

# May 2021

# Mathematics: applications and interpretation

## **Standard level**

Paper 2

16 pages



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## Instructions to Examiners

#### Abbreviations

- *M* Marks awarded for attempting to use a correct **Method**.
- **A** Marks awarded for an **Answer** or for **Accuracy**; often dependent on preceding **M** marks.
- *R* Marks awarded for clear **Reasoning**.
- AG Answer given in the question and so no marks are awarded.
- *FT* Follow through. The practice of awarding marks, despite candidate errors in previous parts, for their correct methods/answers using incorrect results.

#### Using the markscheme

#### 1 General

Award marks using the annotations as noted in the markscheme eg M1, A2.

## 2 Method and Answer/Accuracy marks

- Do **not** automatically award full marks for a correct answer; all working **must** be checked, and marks awarded according to the markscheme.
- It is generally not possible to award *M0* followed by *A1*, as *A* mark(s) depend on the preceding *M* mark(s), if any.
- Where *M* and *A* marks are noted on the same line, *e.g. M1A1*, this usually means *M1* for an **attempt** to use an appropriate method (*e.g.* substitution into a formula) and *A1* for using the **correct** values.
- Where there are two or more **A** marks on the same line, they may be awarded independently; so if the first value is incorrect, but the next two are correct, award **A0A1A1**.
- Where the markscheme specifies A3, M2 etc., do not split the marks, unless there is a note.
- The response to a "show that" question does not need to restate the *AG* line, unless a **Note** makes this explicit in the markscheme.
- Once a correct answer to a question or part question is seen, ignore further working even if this
  working is incorrect and/or suggests a misunderstanding of the question. This will encourage a
  uniform approach to marking, with less examiner discretion. Although some candidates may be
  advantaged for that specific question item, it is likely that these candidates will lose marks
  elsewhere too.
- An exception to the previous rule is when an incorrect answer from further working is used in a subsequent part. For example, when a correct exact value is followed by an incorrect decimal approximation in the first part and this approximation is then used in the second part. In this situation, award *FT* marks as appropriate but do not award the final *A1* in the first part. Examples:

	Correct answer seen	Further working seen	Any FT issues?	Action
1.	$8\sqrt{2}$	5.65685 (incorrect decimal value)	No. Last part in question.	Award <b>A1</b> for the final mark (condone the incorrect further working)
2.	$\frac{35}{72}$	0.468111… (incorrect decimal value)	Yes. Value is used in subsequent parts.	Award <b>A0</b> for the final mark (and full <b>FT</b> is available in subsequent parts)

#### 3 Implied marks

Implied marks appear in **brackets e.g.** (*M1*), and can only be awarded if **correct** work is seen or implied by subsequent working/answer.

#### 4 Follow through marks (only applied after an error is made)

Follow through (*FT*) marks are awarded where an incorrect answer from one **part** of a question is used correctly in **subsequent** part(s) (e.g. incorrect value from part (a) used in part (d) or incorrect value from part (c)(i) used in part (c)(ii)). Usually, to award *FT* marks, **there must be working present** and not just a final answer based on an incorrect answer to a previous part. However, if all the marks awarded in a subsequent part are for the answer or are implied, then *FT* marks should be awarded for *their* correct answer, even when working is not present.

**For example**: following an incorrect answer to part (a) that is used in subsequent parts, where the markscheme for the subsequent part is *(M1)A1*, it is possible to award full marks for *their* correct answer, **without working being seen**. For longer questions where all but the answer marks are implied this rule applies but may be overwritten by a **Note** in the Markscheme.

- Within a question part, once an **error** is made, no further **A** marks can be awarded for work which uses the error, but **M** marks may be awarded if appropriate.
- If the question becomes much simpler because of an error then use discretion to award fewer *FT* marks, by reflecting on what each mark is for and how that maps to the simplified version.
- If the error leads to an inappropriate value (*e.g.* probability greater than 1,  $\sin \theta = 1.5$ , non-integer value where integer required), do not award the mark(s) for the final answer(s).
- The markscheme may use the word "their" in a description, to indicate that candidates may be using an incorrect value.
- If the candidate's answer to the initial question clearly contradicts information given in the question, it is not appropriate to award any *FT* marks in the subsequent parts. This includes when candidates fail to complete a "show that" question correctly, and then in subsequent parts use their incorrect answer rather than the given value.
- Exceptions to these *FT* rules will be explicitly noted on the markscheme.
- If a candidate makes an error in one part but gets the correct answer(s) to subsequent part(s), award marks as appropriate, unless the command term was "Hence".

#### 5 Mis-read

If a candidate incorrectly copies values or information from the question, this is a mis-read (*MR*). A candidate should be penalized only once for a particular misread. Use the *MR* stamp to indicate that this has been a misread and do not award the first mark, even if this is an *M* mark, but award all others as appropriate.

- If the question becomes much simpler because of the *MR*, then use discretion to award fewer marks.
- If the *MR* leads to an inappropriate value (*e.g.* probability greater than 1,  $\sin \theta = 1.5$ , non-integer value where integer required), do not award the mark(s) for the final answer(s).
- Miscopying of candidates' own work does **not** constitute a misread, it is an error.
- If a candidate uses a correct answer, to a "show that" question, to a higher degree of accuracy than given in the question, this is NOT a misread and full marks may be scored in the subsequent part.
- *MR* can only be applied when work is seen. For calculator questions with no working and incorrect answers, examiners should **not** infer that values were read incorrectly.

#### 6 Alternative methods

Candidates will sometimes use methods other than those in the markscheme. Unless the question specifies a method, other correct methods should be marked in line with the markscheme. If the command term is 'Hence' and not 'Hence or otherwise' then alternative methods are not permitted unless covered by a note in the mark scheme.

- Alternative methods for complete questions are indicated by **METHOD 1**, **METHOD 2**, *etc*.
- Alternative solutions for parts of questions are indicated by **EITHER** ... OR.

#### 7 Alternative forms

Unless the question specifies otherwise, accept equivalent forms.

- As this is an international examination, accept all alternative forms of **notation** for example 1.9 and 1,9 or 1000 and 1,000 and 1,000.
- Do not accept final answers written using calculator notation. However, **M** marks and intermediate A marks can be scored, when presented using calculator notation, provided the evidence clearly reflects the demand of the mark.
- In the markscheme, equivalent **numerical** and **algebraic** forms will generally be written in brackets immediately following the answer.
- In the markscheme, some equivalent answers will generally appear in brackets. Not all equivalent notations/answers/methods will be presented in the markscheme and examiners are asked to apply appropriate discretion to judge if the candidate work is equivalent.

#### 8 Format and accuracy of answers

If the level of accuracy is specified in the question, a mark will be linked to giving the answer to the required accuracy. If the level of accuracy is not stated in the question, the general rule applies to final answers: unless otherwise stated in the question all numerical answers must be given exactly or correct to three significant figures.

Where values are used in subsequent parts, the markscheme will generally use the exact value, however candidates may also use the correct answer to 3 sf in subsequent parts. The markscheme will often explicitly include the subsequent values that come "from the use of 3 sf values".

Simplification of final answers: Candidates are advised to give final answers using good mathematical form. In general, for an A mark to be awarded, arithmetic should be completed, and

any values that lead to integers should be simplified; for example,  $\sqrt{\frac{25}{4}}$  should be written as  $\frac{5}{2}$ . An exception to this is simplifying fractions, where lowest form is not required (although the

numerator and the denominator must be integers); for example,  $\frac{10}{4}$  may be left in this form or

written as  $\frac{5}{2}$ . However,  $\frac{10}{5}$  should be written as 2, as it simplifies to an integer.

Algebraic expressions should be simplified by completing any operations such as addition and multiplication, e.g.  $4e^{2x} \times e^{3x}$  should be simplified to  $4e^{5x}$ , and  $4e^{2x} \times e^{3x} - e^{4x} \times e^{x}$  should be simplified to  $3e^{5x}$ . Unless specified in the question, expressions do not need to be factorized, nor do factorized expressions need to be expanded, so x(x+1) and  $x^2 + x$  are both acceptable.

Please note: intermediate A marks do NOT need to be simplified.

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#### 9 Calculators

A GDC is required for this paper, but If you see work that suggests a candidate has used any calculator not approved for IB DP examinations (eg CAS enabled devices), please follow the procedures for malpractice.

#### 10. Presentation of candidate work

**Crossed out work:** If a candidate has drawn a line through work on their examination script, or in some other way crossed out their work, do not award any marks for that work unless an explicit note from the candidate indicates that they would like the work to be marked.

**More than one solution:** Where a candidate offers two or more different answers to the same question, an examiner should only mark the first response unless the candidate indicates otherwise. If the layout of the responses makes it difficult to judge, examiners should apply appropriate discretion to judge which is "first".

(a)	Quota sampling	A1	[1 mark]
(b)	10(hours)	A1	[1 mark]
(c)	15-7	(M1)	[1 mark]
N	ote: Award <i>M1</i> for 15 and 7 seen.		
L	8	A1	[2 marks]
(d)	indication of a valid attempt to find the upper fence $15+1.5\times 8$	(M1)	
	27	A1	
	25 < 27 (accept equivalent answer in words) Jason is correct	R1 A1	
No	<b>te:</b> Do not award <b><i>R0A1</i></b> . Follow through <b>within</b> this part from <i>their</i> 27, but only if their value is supported by a valid attempt <b>or</b> clearly and correctly explains what their value represents.		[4 marks]
(e)	"negative" seen	A1	[
N	ote: Strength cannot be inferred visually; ignore "strong" or "weak".		
			[1 mark]
(f)	correct substitution $y = -1.54 \times 1.5 + 98.8$	(M1)	
	96.5 (%) (96.49)	A1	
	J0.J (70) (70.+7)		[2 marks]
(g)	not reliable extrapolation <b>OR</b> outside the given range of the data	A1 R1	[2 marks]

- 8 -

continued...

#### Question 1 continued

#### (h)

	Book							
	Α	В	С	D	Ε	F	G	Н
Rank – Number of pages	1	3	5	2	6	8	4	7
Rank – Top 50 Rating	1	2	3	4	5	6	7	8
							A1A1	

**Note:** Award **A1** for correct ranks for 'number of pages'. Award **A1** for correct ranks for 'top 50 rating'.

## [2 marks]

A2

#### (i) (i) 0.714 (0.714285...)

**Note:** *FT* from their table.

#### (ii) **EITHER**

there is a (strong/moderate) positive association between the number of pages and the top 50 rating.

#### OR

there is a (strong/moderate) agreement between the rank order of number of pages and the rank order top 50 rating.

#### OR

there is a (strong/moderate) positive (linear) correlation between the rank order of number of pages and the rank order top 50 rating. **A1** 

**Note:** Follow through from their value of  $r_s$ .

[3 marks]

Total [18 marks]

(a) 
$$4 \times \frac{360^{\circ}}{12}$$
 OR  $4 \times 30^{\circ}$  (M1)  
120° A1  
[2 marks]  
(b) substitution in cosine rule (M1)  
 $AB^{2} = 10^{2} + 6^{2} - 2 \times 10 \times 6 \times \cos(120^{\circ})$  (A1)  
 $AB = 14 \text{ cm}$  A1  
Note: Follow through marks in part (b) are contingent on working seen. [3 marks]  
(c)  $\theta = 13 \times 6$  (M1)  
 $= 78^{\circ}$  A1  
(d) substitution into the formula for arc length  
 $l = \frac{78}{360} \times 2 \times \pi \times 10$  OR  $l = \frac{13\pi}{30} \times 10$   
 $= 13.6 \text{ cm} \left( 13.6135..., 4.33\pi, \frac{13\pi}{3} \right)$  [2 marks]  
(e) substitution into the area of a sector  
 $A = \frac{78}{360} \times \pi \times 10^{2}$  OR  $l = \frac{1}{2} \times \frac{13\pi}{30} \times 10^{2}$   
 $= 68.1 \text{ cm}^{2} \left( 68.0678..., 21.7\pi, \frac{65\pi}{3} \right)$  A1  
[2 marks]  
(f) 23 A1  
[1 mark]

continued...

– 10 –

2.

### Question 2 continued

(g)
 correct substitution
 (M1)

 
$$h = 10 \cos(160^\circ) + 13$$
 41

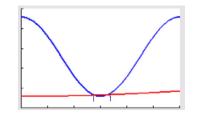
  $= 3.60 \text{ cm} (3.60307...)$ 
 A1

[2 marks]

[1 mark]

(i) EITHER  $10 \times \cos(\theta) + 13 = -10 \times \cos\left(\frac{\theta}{12}\right) + 13$  (M1)

OR



(M1)

A1

**Note:** Award *M1* for equating the functions. Accept a sketch of  $h(\theta)$  and  $g(\theta)$  with point(s) of intersection marked.

THEN

 $k = 196^{\circ}$  (196.363...)

Note: The answer 166.153... is incorrect but the correct method is implicit. Award (M1)A0.

[2 marks]

Total [17 marks]

### 3. (a) EITHER

N = 2  $PV = -37\,000$  I% = 6.4 P/Y = 1C/Y = 4

(M1)(A1)

**Note:** Award *M1* for an attempt to use a financial app in their technology, award *A1* for all entries correct.

#### OR

N = 8  $PV = -37\,000$  I% = 6.4 P/Y = 4C/Y = 4

#### (M1)(A1)

(M1)(A1)

A1

[3 marks]

**Note:** Award *M1* for an attempt to use a financial app in their technology, award *A1* for all entries correct.

OR

$$FV = 37\,000 \times \left(1 + \frac{6.4}{100 \times 4}\right)^{4 \times 2}$$

**Note:** Award *M1* for substitution into compound interest formula, *(A1)* for correct substitution.

= 42 010 AUD

**Note:** Award *(M1)(A1)A0* for unsupported 42009.87.

(b) **EITHER**  $PV = -37\,000$ 

 $FV = 50\,000$ I% = 6.4P/Y = 1C/Y = 4

(M1)(A1)

**Note:** Award *M1* for an attempt to use a financial app in their technology, award *A1* for all entries correct. The final mark can still be awarded for the correct number of months (multiple of 3).

continued...

**Question 3 continued** 

OR	
PV = -37000	
FV = 50000	
I% = 6.4	
P/Y = 4	
C/Y = 4	<u>(M1)(</u> A1)

**Note:** Award *M1* for an attempt to use a financial app in their technology, award *A1* for all entries correct.

#### OR

$$50000 < 37000 \times \left(1 + \frac{6.4}{100 \times 4}\right)^{4 \times n} \text{ OR } 50000 < 37000 \times \left(1 + \frac{6.4}{100 \times 4}\right)^{n} \text{ (M1)(A1)}$$
Note: Award **M1** for the correct inequality, 50000 and substituted compound interest formula. Allow an equation. Award **A1** for correct substitution.

THEN

N = 4.74 (years) (4.74230...) **OR** N = 18.9692... (quarters) (A1)

m = 57 months

**Note:** Award **A1** for rounding their m to the correct number of months. The final answer must be a multiple of 3. Follow through within this part.

[4 marks]

(c) 150000 AUD

[1 mark]

A1

A1

continued...

000 <b>(M1)</b>	(i)	(d) (
A1		
(M1)(A1)	(ii)	(
ttempt to use a financial app in their technology or an annuity formula or $FV = 0$ seen. If a compound interest to zero, award <b>M1</b> , otherwise award <b>M0</b> for a substituted formula.	a fo	Note

$$r = 6.46 (\%) (6.45779...)$$

A1

(e) N = 60

I = 6.46 (6.45779...) PV = -150000 PMT = 1700 P/Y = 12C/Y = 12

**Note:** Award *M1* for an attempt to use a financial app in their technology or an attempt to use an annuity formula. Award *(M0)* for a substituted compound interest formula. Award *A1* for all entries correct. Follow through marks in part (e) are contingent on working seen.

*FV* = 86973 AUD

A1

(M1)(A1)

[3 marks]

(f)  $204000 - (60 \times 1700 + 86973)$  OR 204000 - 188973 (M1)(M1) Note: Award M1 for  $60 \times 1700$ . Award M1 for subtracting their  $(60 \times 1700 + 86973)$  from their (204000). Award at most M1M0 for their  $204000 - (60 \times 1700)$  or M0M0 for their 204000 - (86973). Follow through from parts (d)(i) and (e). Follow through marks in part (f) are contingent on working seen.

15027 AUD

A1 [3 marks] Total [19 marks]

(b) (i) multiplying their probability by 1000 $451.7$ (M1) A1(ii) 510.5A1 (3 mailNote: Answers should be given to 4 sf.[3 mail](c) $H_0$ : stopping distances can be modelled by $N(6.76, 0.12^2)$ $H_1$ : stopping distances cannot be modelled by $N(6.76, 0.12^2)$ A1A1Note: Award A1 for correct $H_0$ , including reference to the mean and standard deviation. Award A1 for the negation of their $H_0$ .[2 mail](d) 15.1 or 22.8 seen $0.0727$ (0.0726542, 7.27%)A2	(a)	(i)	evidence of correct probability e.g sketch <b>OR</b> correct probability statement, $P(X < 6.5)$	<b>(M1)</b> )	
Note: Answers should be given to 4 decimal place.       [3 main state in [3 main sta			0.0151	A1	
[3 main constraints]       [3 main constraints]         (b) (i) multiplying their probability by 1000 (M1) A1       A1         (ii) 510.5       A1         (iii) 510.5       A1         Note: Answers should be given to 4 sf.       [3 main constraints]         (c) $H_0$ : stopping distances can be modelled by $N(6.76, 0.12^2)$ A1A1         Note: Answers constraints are modelled by $N(6.76, 0.12^2)$ A1A1         Note: Award A1 for correct $H_0$ , including reference to the mean and standard deviation. Award A1 for the negation of their $H_0$ .       [2 main constraints]         (d) 15.1 or 22.8 seen       (M1)       0.0727 (0.0726542, 7.27%)         (e) $0.05 < 0.0727$ R1		(ii)	0.0228	A1	
(b) (i) multiplying their probability by 1000       (M1) A1         (ii) 510.5       A1         (iii) 510.5       A1         Note: Answers should be given to 4 sf.       [3 main content of the state of the stat	Not	te: A	nswers should be given to 4 decimal place.		
451.7       A1         (ii) 510.5       A1         (ii) 510.5       A1         Note: Answers should be given to 4 sf.       [3 main content of a standard be given to 4 sf.]         (c) $H_0$ : stopping distances can be modelled by $N(6.76, 0.12^2)$ A1A1         Note: Award A1 for correct $H_0$ , including reference to the mean and standard deviation. Award A1 for the negation of their $H_0$ .       [2 main content of a standard deviation. Award A1 for the negation of their $H_0$ .         (d) 15.1 or 22.8 seen       (M1)       0.0727 (0.0726542, 7.27%)       A2         [3 main content of the standard content of the standard the stand	L				[3 mai
[3 main for the negation of their H <sub>0</sub> .         (c)       H <sub>0</sub> : stopping distances can be modelled by N(6.76, 0.12 <sup>2</sup> )         H <sub>1</sub> : stopping distances cannot be modelled by N(6.76, 0.12 <sup>2</sup> )         A1A1         Note: Award A1 for correct H <sub>0</sub> , including reference to the mean and standard deviation.         Award A1 for the negation of their H <sub>0</sub> .         [2 main for the negation of their H <sub>0</sub> .         (d)       15.1 or 22.8 seen         (M1)         0.0727       (0.0726542, 7.27%)         A2         [3 main for the	(b)	(i)		• • •	
Note: Answers should be given to 4 sf.(c) $H_0$ : stopping distances can be modelled by $N(6.76, 0.12^2)$ $H_1$ : stopping distances cannot be modelled by $N(6.76, 0.12^2)$ A1A1Note: Award A1 for correct $H_0$ , including reference to the mean and standard deviation. Award A1 for the negation of their $H_0$ .[2 mathematical content of the standard deviation. (M1) 0.0727 (0.0726542, 7.27%)(e) $0.05 < 0.0727$ R1		(ii)	510.5	A1	
Award A1 for the negation of their $H_0$ .       [2 mathematical math		H <sub>1</sub> :	stopping distances cannot be modelled by $N(6.76, 0.12^2)$		tion
(d) $15.1 \text{ or } 22.8 \text{ seen}$ (M1) 0.0727  (0.0726542, 7.27%) A2 [3 ma] (e) $0.05 < 0.0727$ R1	NO			i standard devia	luon.
$\begin{array}{c} 0.0727 & (0.0726542, 7.27\%) \\ (e) & 0.05 < 0.0727 \\ \end{array} \qquad \qquad$					[2 ma
(e) 0.05 < 0.0727 <b>R1</b>	(d)	15			1
	( )	15	1 or 22.8 seen	(M1)	1
there is insufficient evidence to reject $H_0$ (or "accept $H_0$ ") A1	( )				[3 mai
		0.0	0727 (0.0726542, 7.27%)	A2	-
	(e)	0.0 0.05 there	(0.0726542, 7.27%) 5 < 0.0727	A2 R1	-

[2 marks] Total [13 marks] (a) (i) evidence of power rule (at least one correct term seen) (M1)  $\frac{dy}{dx} = -0.3x^2 + 1.6x$ A1

(ii) 
$$-0.3x^2 + 1.6x = 0$$
 **M1**

$$x = 5.33 \left( 5.33333..., \frac{16}{3} \right)$$

$$y = -0.1 \times 5.33333...^{3} + 0.8 \times 5.33333...^{2}$$
 (M1)  
Note: Award M1 for substituting their zero for  $\frac{dy}{dx}$  (5.333...) into y.

**Note:** Award *M0A0M0A0* for an unsupported 7.59. Award at most *M0A0M1A0* if only the last two lines in the solution are seen. Award at most *M1A0M1A1* if their x = 5.33 is not seen.

(b) 
$$A = \frac{1}{2} \times 2((2.4+0) + 2(6.4+7.2))$$
 (A1)(M1)

**Note:** Award **A1** for h = 2 seen. Award **M1** for correct substitution into the trapezoidal rule (the zero can be omitted in working).

$$= 29.6 \text{ m}^2$$

5.

A1

A1

[3 marks]

A2

(c) (i) 
$$A = \int_{2}^{8} -0.1x^{3} + 0.8x^{2} dx$$
 OR  $A = \int_{2}^{8} y dx$  A1A1  
Note: Award A1 for a correct integral, A1 for correct limits in the correct location

**Note:** Award **A1** for a correct integral, **A1** for correct limits in the correct location. Award at most **A0A1** if dx is omitted.

(ii)  $A = 32.4 \text{ m}^2$ **Note:** As per the marking instructions, *FT* from the

**Note:** As per the marking instructions, *FT* from their integral in part (c)(i). Award at most *A1FTA0* if their area is >48, this is outside the constraints of the question (a 6x8 rectangle).

[4 marks]

Total [13 marks]