Arcs and sectors [37 marks]

1. This diagram shows a metallic pendant made out of four equal sectors of [4 marks] a larger circle of radius OB = 9 cm and four equal sectors of a smaller circle of radius OA = 3 cm. The angle $BOC = 20^{\circ}$.



Find the area of the pendant.

Consider the following diagram.



The sides of the equilateral triangle ABC have lengths 1 m. The midpoint of [AB] is denoted by P. The circular arc AB has centre, M, the midpoint of [CP].

2a. Find AM.	[3 marks]
^{b.} Find $\operatorname{A}\overset{\wedge}{\operatorname{M}}\operatorname{P}$ in radians.	[2 marks]

3. Boat A is situated 10km away from boat B, and each boat has a marine [6 marks] radio transmitter on board. The range of the transmitter on boat A is 7km, and the range of the transmitter on boat B is 5km. The region in which both transmitters can be detected is represented by the shaded region in the following diagram. Find the area of this region.



The following shape consists of three arcs of a circle, each with centre at the opposite vertex of an equilateral triangle as shown in the diagram.



For this shape, calculate

4a. the perimeter.

[2 marks]

5. A sector of a circle with radius r cm, where r > 0, is shown on the [4 marks] following diagram. The sector has an angle of 1 radian at the centre.



Let the area of the sector be $A \operatorname{cm}^2$ and the perimeter be $P \operatorname{cm}$. Given that A = P, find the value of r.

The diagram shows two circles with centres at the points A and B and radii 2r and r, respectively. The point B lies on the circle with centre A. The circles intersect at the points C and D.



Let α be the measure of the angle CAD and θ be the measure of the angle CBD in radians.

6a. Find an expression for the shaded area in terms of α , θ and r. [3 marks]

6b. Show that $\alpha = 4 \arcsin \frac{1}{4}$.

[2 marks]

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