

1b. Find the area of triangle ABC.

[2 marks]

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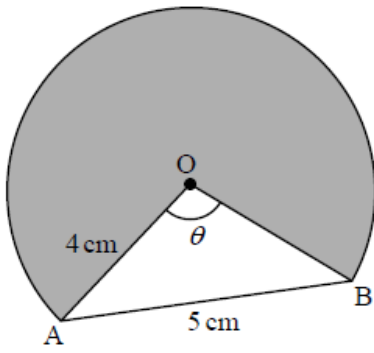
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The following diagram shows part of a circle with centre O and radius 4 cm.



Chord AB has a length of 5 cm and $\widehat{AOB} = \theta$.

2a. Find the value of θ , giving your answer in radians.

[3 marks]

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2b. Find the area of the shaded region.

[3 marks]

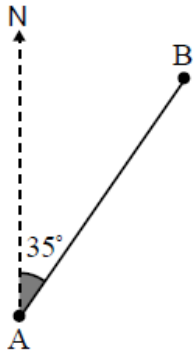
A large rectangular box with a solid black border, intended for a student's answer. Inside the box, there are six horizontal dotted lines spaced evenly from top to bottom, providing a guide for writing.

Adam sets out for a hike from his camp at point A. He hikes at an average speed of 4.2 km/h for 45 minutes, on a bearing of 035° from the camp, until he stops for a break at point B.

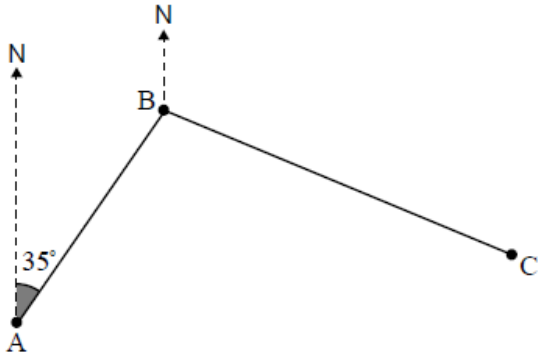
3a. Find the distance from point A to point B.

[2 marks]

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Adam leaves point B on a bearing of 114° and continues to hike for a distance of 4.6 km until he reaches point C.



3b. Show that $\hat{A}BC$ is 101° .

[2 marks]

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3c. Find the distance from the camp to point C.

[3 marks]

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3d. Find \hat{BCA} .

[3 marks]

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3f. Jacob hikes at an average speed of 3.9 km/h.

[3 marks]

Find, to the nearest minute, the time it takes for Jacob to reach point C.

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Consider a function f , such that $f(x) = 5.8 \sin\left(\frac{\pi}{6}(x + 1)\right) + b$, $0 \leq x \leq 10$,
 $b \in \mathbb{R}$.

4a. Find the period of f .

[2 marks]

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The function f has a local maximum at the point $(2, 21.8)$, and a local minimum at $(8, 10.2)$.

4b. Find the value of b .

[2 marks]

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4c. Hence, find the value of $f(6)$.

[2 marks]

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4e. Find the value of x for which the functions have the greatest difference. [2 marks]

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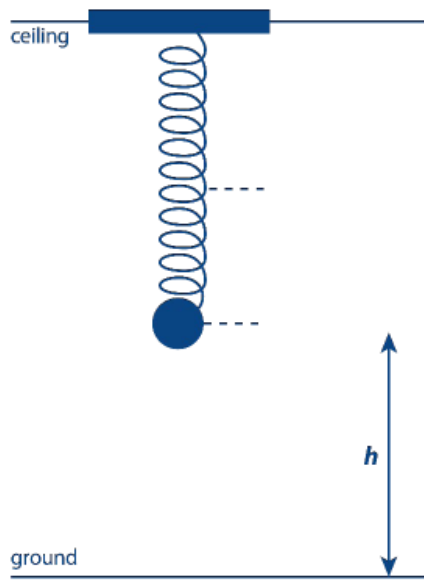
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The following diagram shows a ball attached to the end of a spring, which is suspended from a ceiling.



The height, h metres, of the ball above the ground at time t seconds after being released can be modelled by the function $h(t) = 0.4 \cos(\pi t) + 1.8$ where $t \geq 0$.

5a. Find the height of the ball above the ground when it is released. *[2 marks]*

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5b. Find the minimum height of the ball above the ground.

[2 marks]

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5c. Show that the ball takes 2 seconds to return to its initial height above the ground for the first time.

[2 marks]

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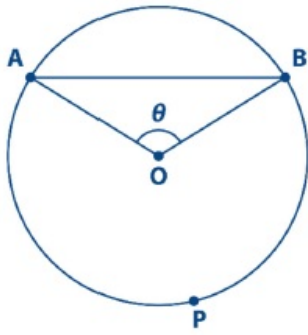
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The following diagram shows a circle with centre O and radius 3 .



Points A , P and B lie on the circumference of the circle.

Chord $[AB]$ has length L and $\widehat{AOB} = \theta$ radians.

6a. Show that arc APB has length $6\pi - 3\theta$.

[2 marks]

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6b. Show that $L = \sqrt{18 - 18 \cos \theta}$.

[2 marks]

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6c. Arc APB is twice the length of chord $[AB]$.

[3 marks]

Find the value of θ .

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Consider $f(x) = 4 \sin x + 2.5$ and $g(x) = 4 \sin\left(x - \frac{3\pi}{2}\right) + 2.5 + q$, where $x \in \mathbb{R}$ and $q > 0$.

The graph of g is obtained by two transformations of the graph of f .

7a. Describe these two transformations.

[2 marks]

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8b. Find the area of this piece of land.

[2 marks]

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8c. Find \hat{CAB} .

[3 marks]

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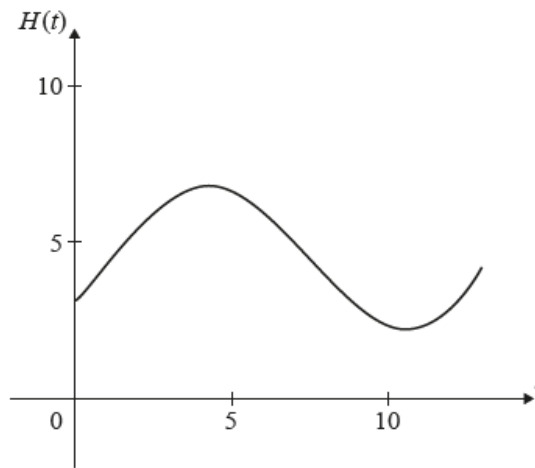
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The height of water, in metres, in Dungeness harbour is modelled by the function $H(t) = a \sin(b(t - c)) + d$, where t is the number of hours after midnight, and a , b , c and d are constants, where $a > 0$, $b > 0$ and $c > 0$.

The following graph shows the height of the water for 13 hours, starting at midnight.



The first high tide occurs at 04 : 30 and the next high tide occurs 12 hours later. Throughout the day, the height of the water fluctuates between 2.2 m and 6.8 m. All heights are given correct to one decimal place.

10a. Show that $b = \frac{\pi}{6}$. [1 mark]

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10b. Find the value of a . [2 marks]

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10c. Find the value of d .

[2 marks]

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10d. Find the smallest possible value of c .

[3 marks]

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10e. Find the height of the water at 12 : 00.

[2 marks]

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10f. Determine the number of hours, over a 24-hour period, for which the tide is higher than 5 metres.

[3 marks]

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10g. A fisherman notes that the water height at nearby Folkestone harbour [2 marks] follows the same sinusoidal pattern as that of Dungeness harbour, with the exception that high tides (and low tides) occur 50 minutes earlier than at Dungeness.

Find a suitable equation that may be used to model the tidal height of water at Folkestone harbour.

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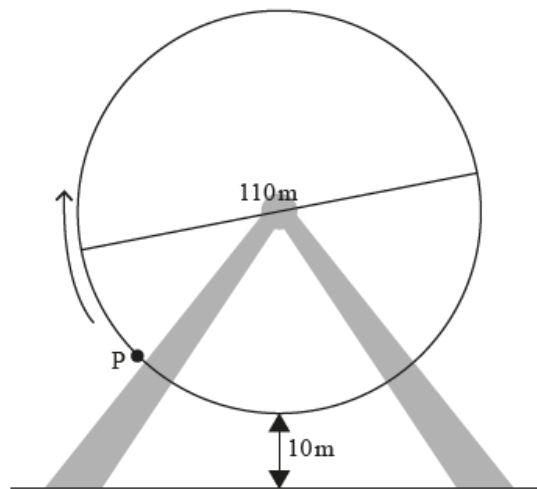
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11. A Ferris wheel with diameter 110 metres rotates at a constant speed. [5 marks] The lowest point on the wheel is 10 metres above the ground, as shown on the following diagram. P is a point on the wheel. The wheel starts moving with P at the lowest point and completes one revolution in 20 minutes.

diagram not to scale

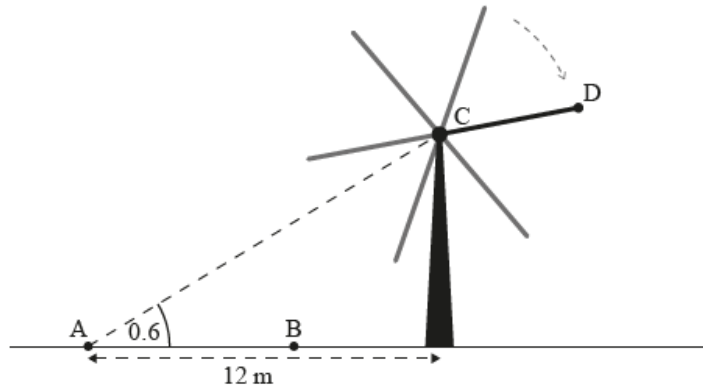


The height, h metres, of P above the ground after t minutes is given by $h(t) = a \cos(bt) + c$, where $a, b, c \in \mathbb{R}$.

Find the values of a , b and c .

A rectangular box containing 15 horizontal dotted lines, intended for handwriting practice.

The six blades of a windmill rotate around a centre point C . Points A and B and the base of the windmill are on level ground, as shown in the following diagram.



From point A the angle of elevation of point C is 0.6 radians.

12a. Given that point A is 12 metres from the base of the windmill, find the *[2 marks]* height of point C above the ground.

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An observer walks 7 metres from point A to point B .

12b. Find the angle of elevation of point C from point B . *[2 marks]*

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The observer keeps walking until he is standing directly under point C. The observer has a height of 1.8 metres, and as the blades of the windmill rotate, the end of each blade passes 2.5 metres over his head.

12c. Find the length of each blade of the windmill.

[2 marks]

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One of the blades is painted a different colour than the others. The end of this blade is labelled point D. The height h , in metres, of point D above the ground can be modelled by the function $h(t) = p \cos\left(\frac{3\pi}{10}t\right) + q$, where t is in seconds and $p, q \in \mathbb{R}$. When $t = 0$, point D is at its maximum height.

12d. Find the value of p and the value of q .

[4 marks]

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The following diagram shows a right-angled triangle, ABC , with $AC = 10$ cm, $AB = 6$ cm and $BC = 8$ cm.

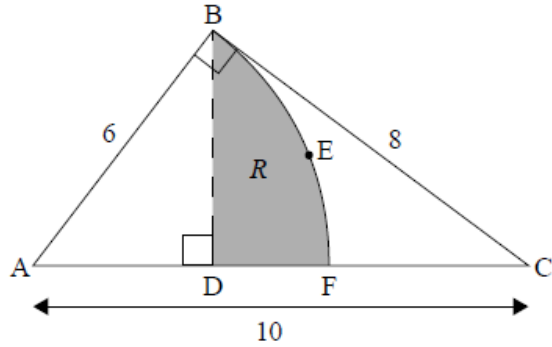
The points D and F lie on $[AC]$.

$[BD]$ is perpendicular to $[AC]$.

BEF is the arc of a circle, centred at A .

The region R is bounded by $[BD]$, $[DF]$ and arc BEF .

diagram not to scale



14a. Find \widehat{BAC} .

[2 marks]

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15b. Find the area, in km^2 , of triangle ABC.

[3 marks]

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16b. A second truck arrives whose ladder, when fully extended, is 30 metres [3 marks] long. The base of this ladder is also 4 metres above the ground. For safety reasons, the maximum angle of elevation that the ladder can make is 70° . Find the maximum height on the wall that can be reached by the ladder on the second truck.

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Let $f(x) = 2 \sin(3x) + 4$ for $x \in \mathbb{R}$.

17a. The range of f is $k \leq f(x) \leq m$. Find k and m .

[3 marks]

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Let $g(x) = 5f(2x)$.

17b. Find the range of g .

[2 marks]

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The function g can be written in the form $g(x) = 10 \sin (bx) + c$.

17c. Find the value of b and of c .

[3 marks]

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17d. Find the period of g .

[2 marks]

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17e. The equation $g(x) = 12$ has two solutions where $\pi \leq x \leq \frac{4\pi}{3}$. Find both [3 marks] solutions.

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