



Let  $\sin \theta = \frac{\sqrt{5}}{3}$ , where  $\theta$  is acute.

2a. Find  $\cos \theta$ .

[3 marks]

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2b. Find  $\cos 2\theta$ .

[2 marks]

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3a. Show that  $\log_9 (\cos 2x + 2) = \log_3 \sqrt{\cos 2x + 2}$ .

[3 marks]

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Consider the functions  $f(x) = \sqrt{3}\sin x + \cos x$  where  $0 \leq x \leq \pi$  and  $g(x) = 2x$  where  $x \in \mathbb{R}$ .

4a. Find  $(f \circ g)(x)$ .

[2 marks]

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4b. Solve the equation  $(f \circ g)(x) = 2 \cos 2x$  where  $0 \leq x \leq \pi$ .

[5 marks]

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5a. Show that  $\sin 2x + \cos 2x - 1 = 2 \sin x(\cos x - \sin x)$ .

[2 marks]

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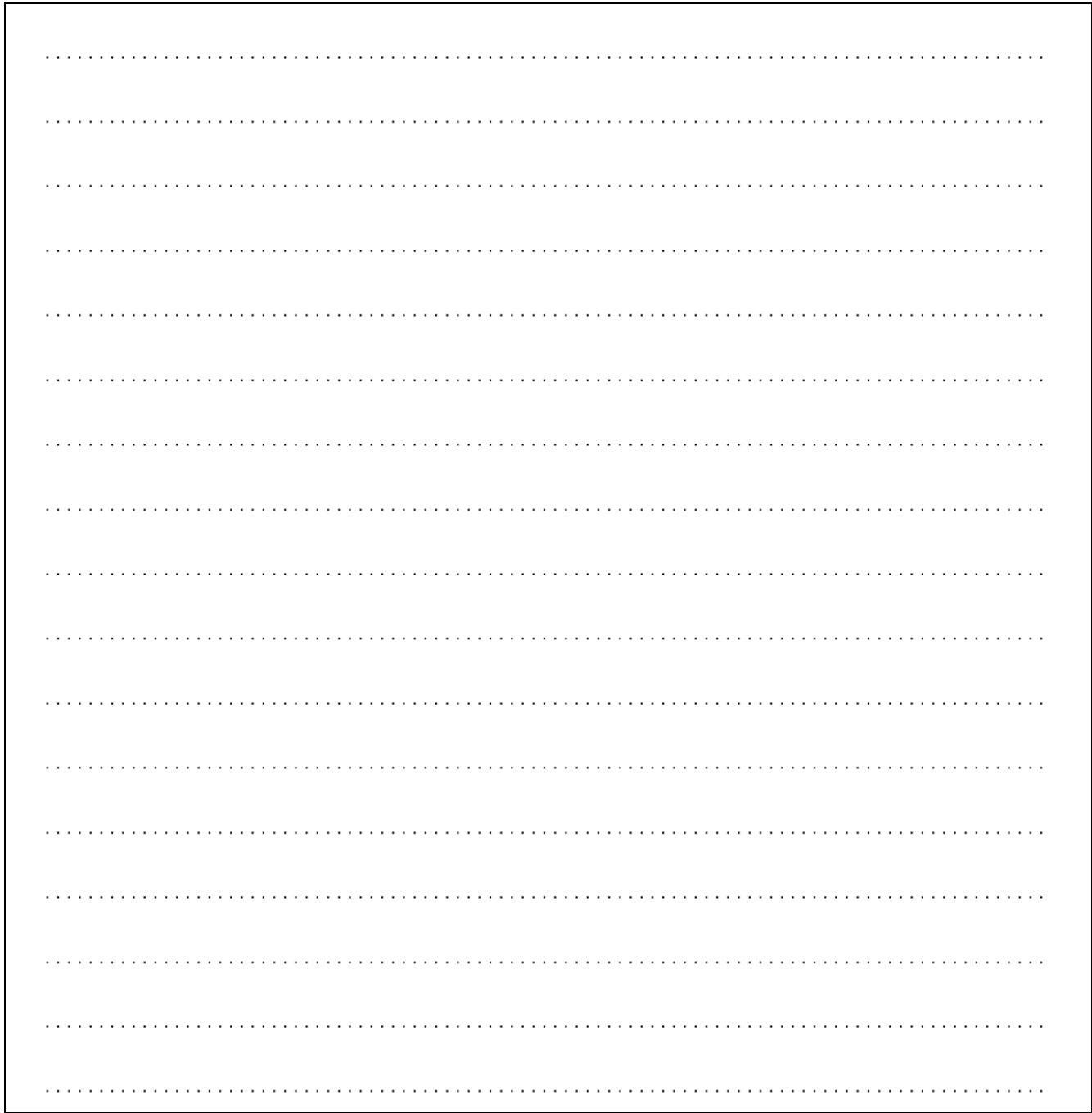
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5b. Hence or otherwise, solve  $\sin 2x + \cos 2x - 1 + \cos x - \sin x = 0$  for  $[6 \text{ marks}]$   
 $0 < x < 2\pi$ .









8. Solve the equation  $2 \cos^2 x + 5 \sin x = 4, 0 \leq x \leq 2\pi$ .

[7 marks]

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9. Let  $f(x) = 4 \cos\left(\frac{x}{2}\right) + 1$ , for  $0 \leq x \leq 6\pi$ . Find the values of  $x$  for which  $f(x) > 2\sqrt{2} + 1$ . [8 marks]





11. Given that  $\sin x = \frac{1}{3}$ , where  $0 < x < \frac{\pi}{2}$ , find the value of  $\cos 4x$ .

[6 marks]

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12. Let  $f(x) = \tan(x + \pi) \cos(x - \frac{\pi}{2})$  where  $0 < x < \frac{\pi}{2}$ .

[5 marks]

Express  $f(x)$  in terms of  $\sin x$  and  $\cos x$ .

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15b. Verify that  $x = \tan \theta$  and  $x = -\cot \theta$  satisfy the equation  
 $x^2 + (2 \cot 2\theta) x - 1 = 0$ .

[7 marks]

A large rectangular box with a solid black border. Inside the box, there are 22 horizontal dotted lines spaced evenly down the page, providing a guide for handwriting the solution to the problem.



15d. Using the results from parts (b) and (c) find the exact value of  $\tan \frac{\pi}{24} - \cot \frac{\pi}{24}$ .

[6 marks]

Give your answer in the form  $a + b\sqrt{3}$  where  $a, b \in \mathbb{Z}$ .

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