## Vectors 10.02 [60 marks]

A line  $L_1$  passes through the points A(0,1,8) and B(3,5,2).

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1b. Hence, write down a vector equation for  $L_1$ .

[2 marks]

1c. A second line  $L_2$ , has equation  $\mathbf{r} = \begin{pmatrix} 1 \\ 13 \\ -14 \end{pmatrix} + s \begin{pmatrix} p \\ 0 \\ 1 \end{pmatrix}$ . [3 marks]

Given that  $L_1$  and  $L_2$  are perpendicular, show that p=2.

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1d. The lines  $L_1$  and  $L_1$  intersect at C(9, 13, z). Find z. [5 marks]

1f. Hence or otherwise, find one point on  $L_2$  which is  $\sqrt{5}$  units from C. [3 marks]

2. Find the Cartesian equation of plane /7 containing the points A (6, 2, 1) [6 marks] and B (3, -1, 1) and perpendicular to the plane x + 2y - z - 6 = 0.

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The points A, B and C have the following position vectors with respect to an origin O.

$$\overrightarrow{OA} = 2\mathbf{i} + \mathbf{j} - 2\mathbf{k}$$
$$\overrightarrow{OB} = 2\mathbf{i} - \mathbf{j} + 2\mathbf{k}$$
$$\overrightarrow{OC} = \mathbf{i} + 3\mathbf{j} + 3\mathbf{k}$$

4a. Find the vector equation of the line (BC).

[3 marks]

4c. Find the Cartesian equation of the plane  $\Pi_1$ , which passes through C and [3 marks] is perpendicular to  $\overrightarrow{OA}$ .

The plane  $\Pi_2$  contains the points O, A and B and the plane  $\Pi_3$  contains the points O, A and C.

4e. Verify that  $2\mathbf{j} + \mathbf{k}$  is perpendicular to the plane  $\Pi_2$ . [3 marks]

4f. Find a vector perpendicular to the plane  $\Pi_3$ .

[1 mark]


5. Find the coordinates of the point of intersection of the planes defined by [5 marks] the equations x + y + z = 3, x - y + z = 5 and x + y + 2z = 6.

Consider the lines  $l_1$  and  $l_2$  defined by

$$l_1: \mathbf{r} = \begin{pmatrix} -3\\-2\\a \end{pmatrix} + \beta \begin{pmatrix} 1\\4\\2 \end{pmatrix}$$
 and  $l_2: \frac{6-x}{3} = \frac{y-2}{4} = 1-z$  where  $a$  is a constant.

Given that the lines  $l_1$  and  $l_2$  intersect at a point P,

6a. find the value of a;

[4 marks]

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