



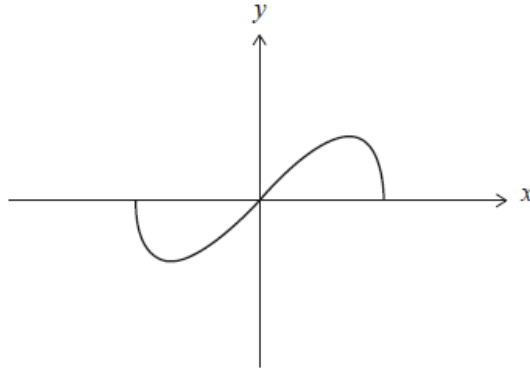






A function  $f$  is defined by  $f(x) = x\sqrt{1-x^2}$  where  $-1 \leq x \leq 1$ .

The graph of  $y = f(x)$  is shown below.



5a. Show that  $f$  is an odd function.

[2 marks]

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Consider the curve  $C$  given by  $y = x - xy \ln(xy)$  where  $x > 0$ ,  $y > 0$ .

6a. Show that  $\frac{dy}{dx} + \left(x \frac{dy}{dx} + y\right)(1 + \ln(xy)) = 1$ .

[3 marks]

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Let  $y = \frac{\ln x}{x^4}$  for  $x > 0$ .

8a. Show that  $\frac{dy}{dx} = \frac{1-4\ln x}{x^5}$ .

[3 marks]

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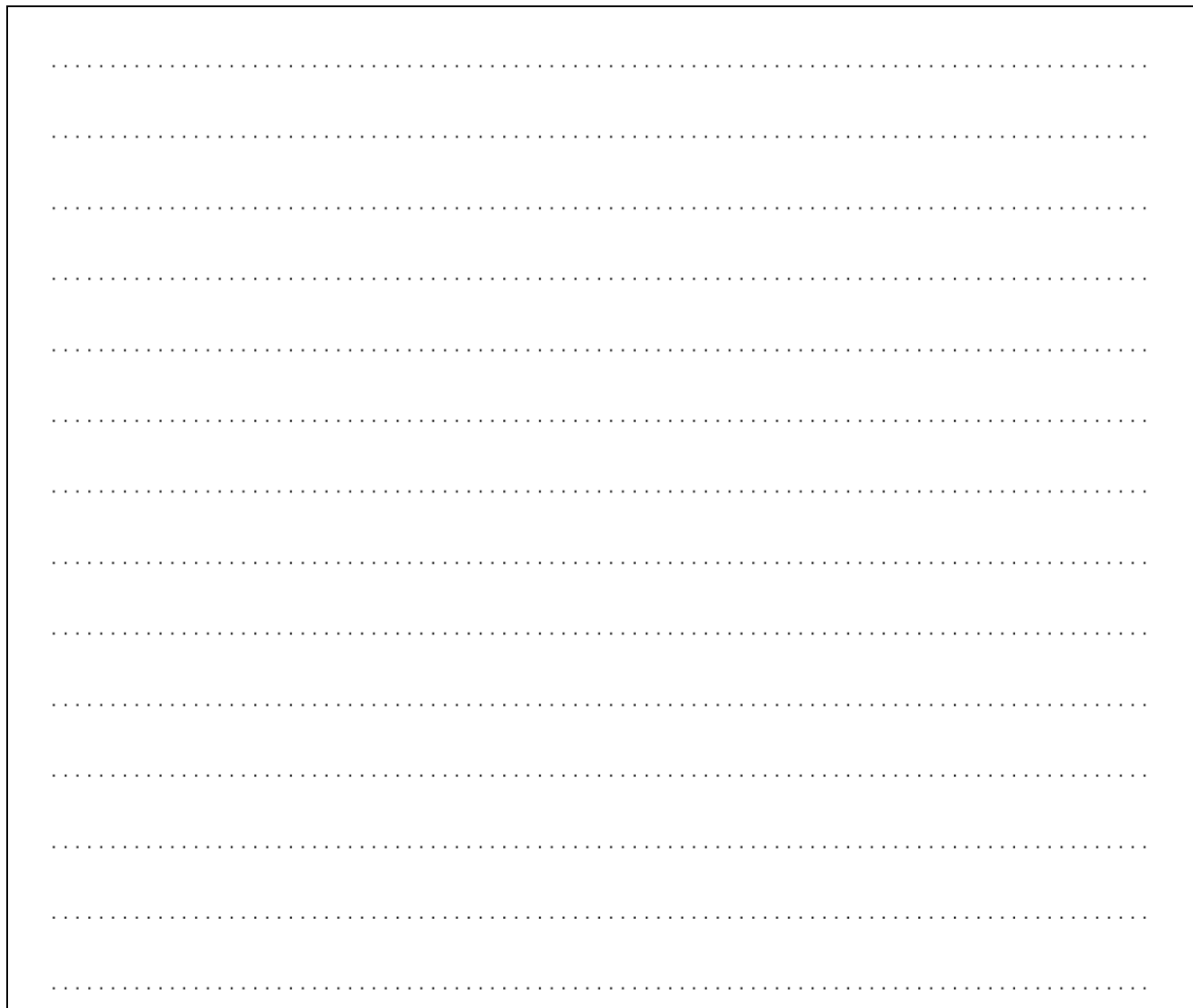
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Consider the function defined by  $f(x) = \frac{\ln x}{x^4}$  for  $x > 0$  and its graph  $y = f(x)$ .

8b. The graph of  $f$  has a horizontal tangent at point  $P$ . Find the coordinates [5 marks] of  $P$ .



8c. Given that  $f''(x) = \frac{20\ln x - 9}{x^6}$ , show that P is a local maximum point. [3 marks]

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8d. Solve  $f(x) > 0$  for  $x > 0$ . [2 marks]

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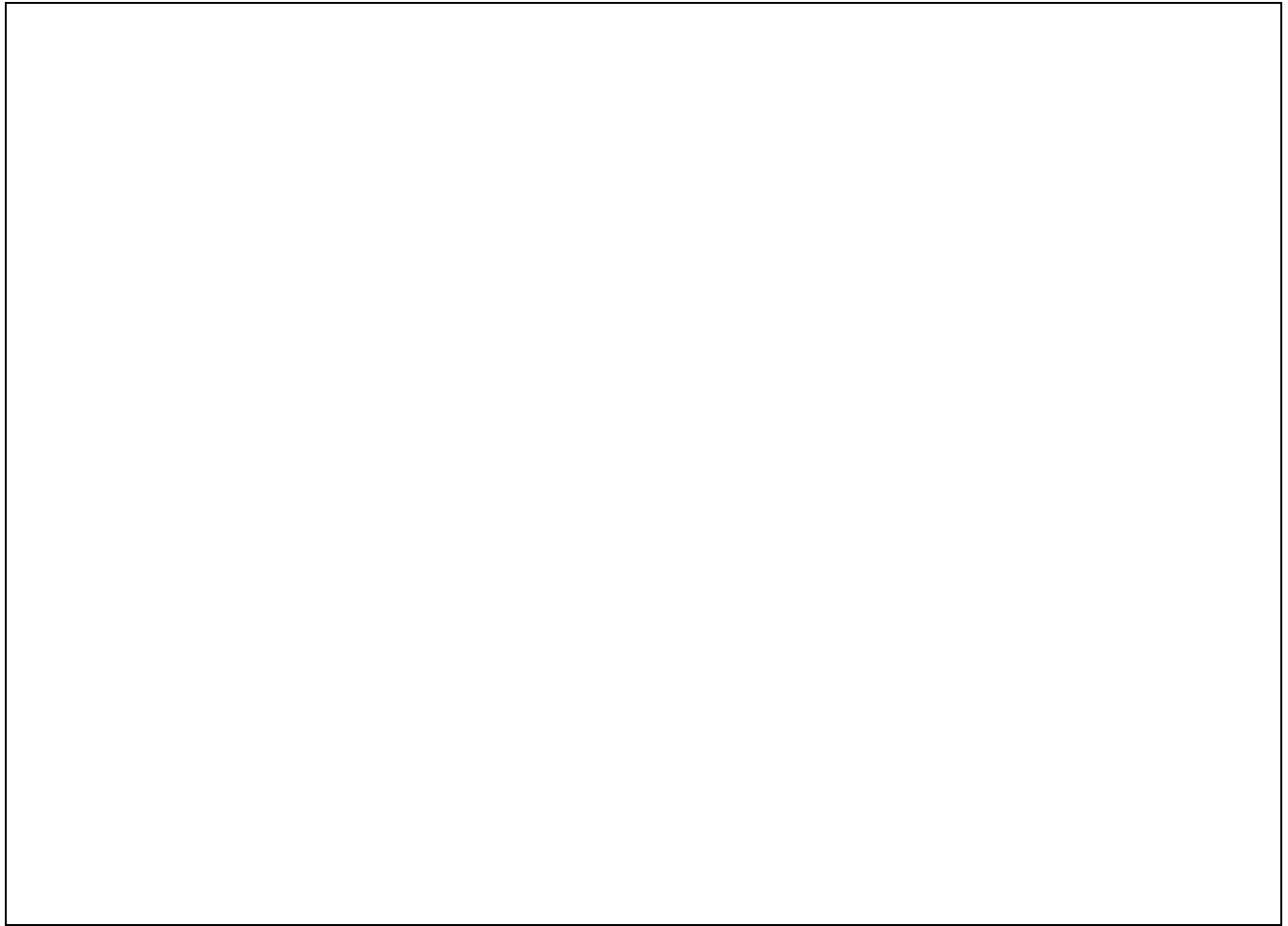
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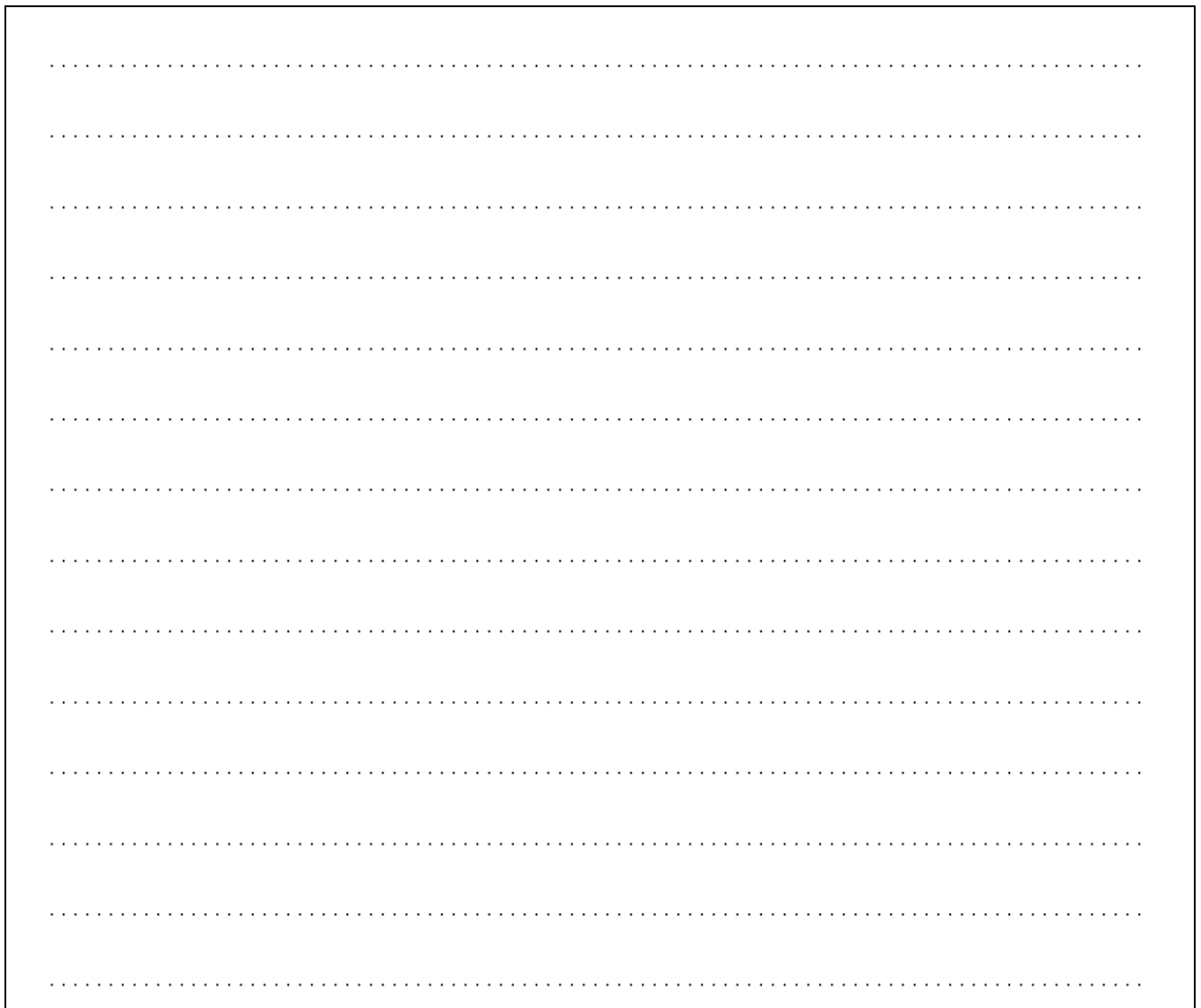
8e. Sketch the graph of  $f$ , showing clearly the value of the  $x$ -intercept and the approximate position of point  $P$ . [3 marks]





9b. Given that the gradient of  $L$  is  $\frac{1}{3}$ , find the  $x$ -coordinate of  $B$ .

[6 marks]



A large rectangular box with a solid black border, containing 15 horizontal dotted lines for writing the answer.

Consider the graph of the function  $f(x) = x^2 - \frac{k}{x}$ .

10a. Write down  $f'(x)$ .

[3 marks]

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The equation of the tangent to the graph of  $y = f(x)$  at  $x = -2$  is  $2y = 4 - 5x$ .

10b. Write down the gradient of this tangent.

[1 mark]

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