



2a. Show that  $2x - 3 - \frac{6}{x-1} = \frac{2x^2-5x-3}{x-1}$ ,  $x \in \mathbb{R}$ ,  $x \neq 1$ .

[2 marks]

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2b. Hence or otherwise, solve the equation  $2 \sin 2\theta - 3 - \frac{6}{\sin 2\theta - 1} = 0$  for *[5 marks]*  
 $0 \leq \theta \leq \pi$ ,  $\theta \neq \frac{\pi}{4}$ .

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3a. Show that  $\sin 2x + \cos 2x - 1 = 2 \sin x(\cos x - \sin x)$ . *[2 marks]*

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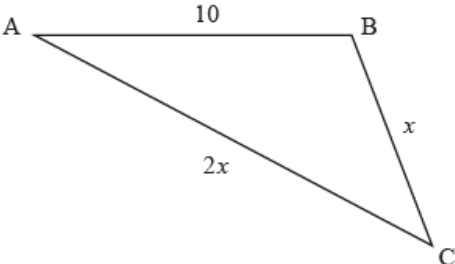
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5. The following diagram shows triangle  $ABC$ , with  $AB = 10$ ,  $BC = x$  and  $AC = 2x$ . [7 marks]

diagram not to scale



Given that  $\cos \hat{C} = \frac{3}{4}$ , find the area of the triangle.

Give your answer in the form  $\frac{p\sqrt{q}}{2}$  where  $p, q \in \mathbb{Z}^+$ .

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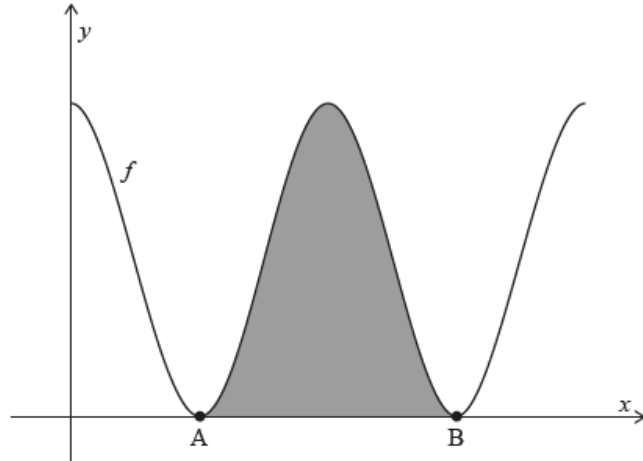
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A large rectangular box containing 15 horizontal dotted lines, intended for writing or drawing.

Consider the function  $f$  defined by  $f(x) = 6 + 6 \cos x$ , for  $0 \leq x \leq 4\pi$ .

The following diagram shows the graph of  $y = f(x)$ .



The graph of  $f$  touches the  $x$ -axis at points **A** and **B**, as shown. The shaded region is enclosed by the graph of  $y = f(x)$  and the  $x$ -axis, between the points **A** and **B**.

6a. Find the  $x$ -coordinates of **A** and **B**.

[3 marks]

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6d. Hence, find the volume of the cone.

[4 marks]

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8b. Show that  $\arctan p + \arctan q \equiv \arctan\left(\frac{p+q}{1-pq}\right)$  where  $p, q > 0$  and  $pq < 1$ . [4 marks]

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8c. Verify that  $\arctan(2x + 1) = \arctan\left(\frac{x}{x+1}\right) + \frac{\pi}{4}$  for  $x \in \mathbb{R}, x > 0$ . [3 marks]

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10b. Find  $\cos(2 \times \widehat{CAB})$ .

[3 marks]

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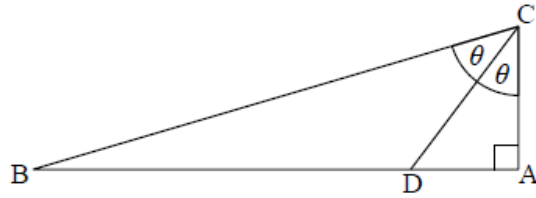
11. Let  $f(x) = 4 \cos\left(\frac{x}{2}\right) + 1$ , for  $0 \leq x \leq 6\pi$ . Find the values of  $x$  for which [8 marks]  
 $f(x) > 2\sqrt{2} + 1$ .





The following diagram shows a right triangle ABC. Point D lies on AB such that CD bisects  $\hat{A}CB$ .

diagram not to scale



$\hat{A}CD = \theta$  and  $AC = 14$  cm

13a. Given that  $\sin \theta = \frac{3}{5}$ , find the value of  $\cos \theta$ .

[3 marks]

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13b. Find the value of  $\cos 2\theta$ .

[3 marks]

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13c. Hence or otherwise, find BC.

[2 marks]

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Let  $\theta$  be an **obtuse** angle such that  $\sin \theta = \frac{3}{5}$ .

14a. Find the value of  $\tan \theta$ .

[4 marks]

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14b. Line  $L$  passes through the origin and has a gradient of  $\tan \theta$ . Find the equation of  $L$ . [2 marks]

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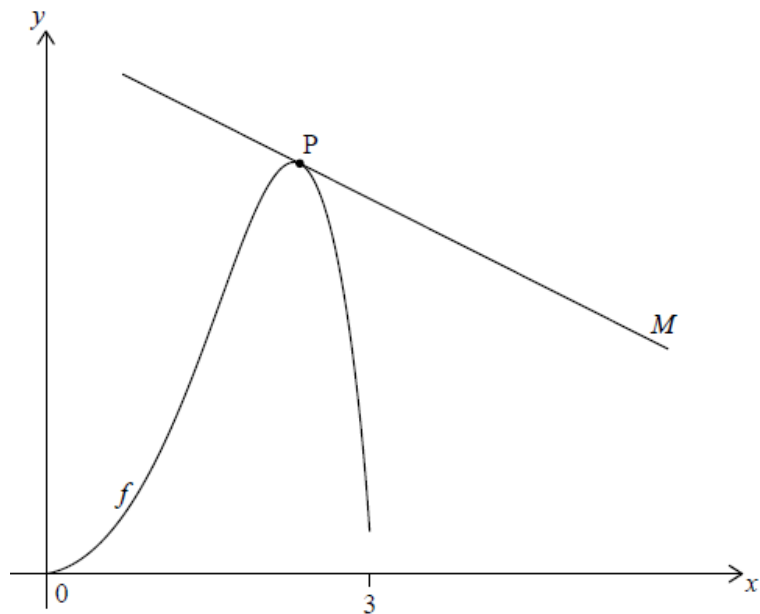
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Let  $f(x) = e^x \sin x - \frac{3x}{4}$ .

14c. The following diagram shows the graph of  $f$  for  $0 \leq x \leq 3$ . Line  $M$  is a [4 marks] tangent to the graph of  $f$  at point P.



Given that  $M$  is parallel to  $L$ , find the  $x$ -coordinate of P.

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The lengths of two of the sides in a triangle are 4 cm and 5 cm. Let  $\theta$  be the angle between the two given sides. The triangle has an area of  $\frac{5\sqrt{15}}{2}$  cm<sup>2</sup>.

15a. Show that  $\sin \theta = \frac{\sqrt{15}}{4}$ .

[1 mark]

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17b. Hence, show that  $\int e^x \cos^2 x dx = \frac{e^x}{5} \sin 2x + \frac{e^x}{10} \cos 2x + \frac{e^x}{2} + c, c \in \mathbb{R}. [3 \text{ marks}]$

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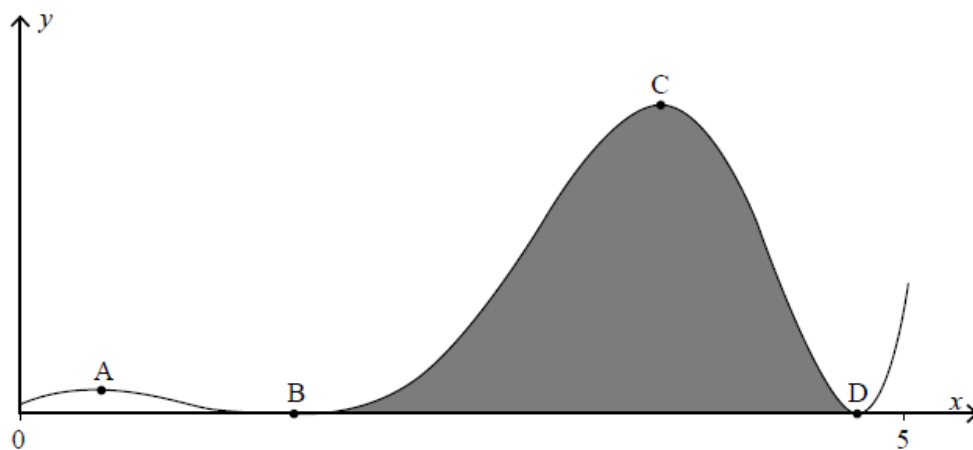
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The function  $f$  is defined by  $f(x) = e^x \cos^2 x$ , where  $0 \leq x \leq 5$ . The curve  $y = f(x)$  is shown on the following graph which has local maximum points at A and C and touches the  $x$ -axis at B and D.



17c. Find the  $x$ -coordinates of A and of C, giving your answers in the form  $a + \arctan b$ , where  $a, b \in \mathbb{R}. [6 \text{ marks}]$

A large rectangular box containing 15 horizontal dotted lines, intended for writing or drawing.



17d. Find the area enclosed by the curve and the  $x$ -axis between B and D, as [5 marks] shaded on the diagram.

A large rectangular box with a solid black border, containing 15 horizontal dotted lines for writing the solution.



Let  $S$  be the sum of the roots found in part (a).

18b. Show that  $\operatorname{Re} S = \operatorname{Im} S$ .

[4 marks]

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18c. By writing  $\frac{\pi}{12}$  as  $\left(\frac{\pi}{4} - \frac{\pi}{6}\right)$ , find the value of  $\cos \frac{\pi}{12}$  in the form  $\frac{\sqrt{a} + \sqrt{b}}{c}$  [3 marks]  
where  $a$ ,  $b$  and  $c$  are integers to be determined.

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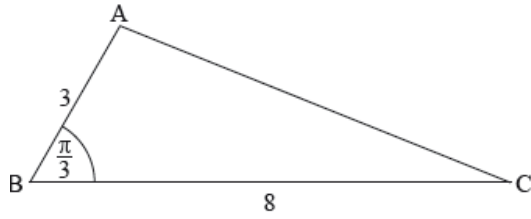
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The following diagram shows triangle ABC, with  $AB = 3\text{cm}$ ,  $BC = 8\text{cm}$ , and  $\hat{A}BC = \frac{\pi}{3}$ .

diagram not to scale



20a. Show that  $AC = 7\text{ cm}$ .

[4 marks]

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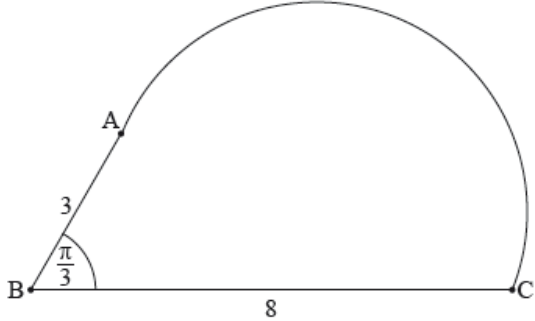
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20b. The shape in the following diagram is formed by adding a semicircle with diameter [AC] to the triangle. [3 marks]

diagram not to scale



Find the exact perimeter of this shape.

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