

Do **not** write solutions on this page.

12. [Maximum mark: 15]

Phil takes out a bank loan of \$150 000 to buy a house, at an annual interest rate of 3.5%. The interest is calculated at the end of each year and added to the amount outstanding.

- (a) Find the amount Phil would owe the bank after 20 years. Give your answer to the nearest dollar. [3]

To pay off the loan, Phil makes annual deposits of \$ $P$  at the end of every year in a savings account, paying an annual interest rate of 2%. He makes his first deposit at the end of the first year after taking out the loan.

- (b) Show that the total value of Phil's savings after 20 years is  $\frac{(1.02^{20} - 1)P}{(1.02 - 1)}$ . [3]

- (c) Given that Phil's aim is to own the house after 20 years, find the value for  $P$  to the nearest dollar. [3]

David visits a different bank and makes a single deposit of \$ $Q$ , the annual interest rate being 2.8%.

- (d) (i) David wishes to withdraw \$5000 at the end of each year for a period of  $n$  years. Show that an expression for the minimum value of  $Q$  is  $\frac{5000}{1.028} + \frac{5000}{1.028^2} + \dots + \frac{5000}{1.028^n}$ . [6]
- (ii) Hence or otherwise, find the minimum value of  $Q$  that would permit David to withdraw annual amounts of \$5000 indefinitely. Give your answer to the nearest dollar.

