

Name:

Result:

Group A

Zadanie 1.

[6 punktów]

Calculate the following limits:

(a) $\lim_{x \rightarrow 1} \frac{x^2 + 2x - 3}{x^5 - 1}$

(b) $\lim_{x \rightarrow 3} \frac{x - 3}{\sqrt{x+1} - \sqrt{3x-5}}$

(c) $\lim_{x \rightarrow 5} \frac{\sqrt[3]{x+3} - 2}{x - 5}$

(d) $\lim_{x \rightarrow -\infty} \frac{\sqrt{9x^2 + x + 11}}{1 - 2x}$

(e) $\lim_{x \rightarrow \infty} (\sqrt{x^2 + 3x} - \sqrt{x^2 + 3})$

(f) $\lim_{x \rightarrow 2^-} \frac{x + 3}{x^2 - 9x + 14}$

Zadanie 2.

[2 punkty]

Find the values of parameters a and b , given that the function:

$$f(x) = \begin{cases} ax + b & \text{if } x < -1 \\ 2^x & \text{if } -1 \leq x \leq 2 \\ ax^2 + b & \text{if } x > 2 \end{cases}$$

is continuous.

Zadanie 3.

[2 punkty]

Prove that the equation:

$$x^4 + 12x + 3 = 2x^3 + 11x^2$$

has at least two solutions in the interval $\langle -1, 2 \rangle$.