Rounding & Standard Form

- Roudning to a given number of decimal places.
- Rounding to a given number of significant figures.
- Converting numbers to standard form.



Given any number there are two predominant ways of rounding it:



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- using a specific number of decimal places (d.p.),

Image: A math a math

Rounding

Given any number there are two predominant ways of rounding it:

- using a specific number of decimal places (d.p.),
- using a specific number of significant figures (s.f.)

Image: A math a math

Rounding - decimal places

When rounding to decimal places we round to a certain position after the decimal point.

When rounding to decimal places we round to a certain position after the decimal point. If the digit immediately past this position is 4 or less we round down, if it's 5 or more we round up.

1 d.p.: 6546.5

- 1 d.p.: 6546.5
- 2 d.p.: 6546.55

- 1 d.p.: 6546.5
- 2 d.p.: 6546.55
- 3 d.p.: 6546.547

- 1 d.p.: 6546.5
- 2 d.p.: 6546.55
- 3 d.p.: 6546.547
- 4 d.p.: 6546.5465

- 1 d.p.: 6546.5
- 2 d.p.: 6546.55
- 3 d.p.: 6546.547
- 4 d.p.: 6546.5465

Note that we can also round this number to:

the nearest unit: 6547

- 1 d.p.: 6546.5
- 2 d.p.: 6546.55
- 3 d.p.: 6546.547
- 4 d.p.: 6546.5465

Note that we can also round this number to:

the nearest unit: 6547

the nearest ten: 6550

- 1 d.p.: 6546.5
- 2 d.p.: 6546.55
- 3 d.p.: 6546.547
- 4 d.p.: 6546.5465

Note that we can also round this number to:

the nearest unit: 6547

the nearest ten: 6550

the nearest hundred: 6500

- 1 d.p.: 6546.5
- 2 d.p.: 6546.55
- 3 d.p.: 6546.547
- 4 d.p.: 6546.5465

Note that we can also round this number to:

the nearest unit: 6547

the nearest ten: 6550

the nearest hundred: 6500

the nearest thousand: 7000

a) 25.519

Image: A math a math

- a) 25.519
 - i. 1 d.p.:

- a) 25.519
 - i. 1 d.p.: 25.5

- a) 25.519
 - i. 1 d.p.: 25.5
 - ii. nearest unit:

イロト イ押ト イヨト イヨ

- a) 25.519
 - i. 1 d.p.: 25.5
 - ii. nearest unit: 26

イロト イ押ト イヨト イヨ

- a) 25.519
 - i. 1 d.p.: 25.5
 - ii. nearest unit: 26
 - iii. 2 d.p.:

- a) 25.519
 - i. 1 d.p.: 25.5
 - ii. nearest unit: 26
 - iii. 2 d.p.: 25.52

Image: A math a math

- a) 25.519
 - i. 1 d.p.: 25.5
 - ii. nearest unit: 26
 - iii. 2 d.p.: 25.52
- b) 321.0990

Image: A math a math

- a) 25.519
 - i. 1 d.p.: 25.5
 - ii. nearest unit: 26
 - iii. 2 d.p.: 25.52
- b) 321.0990
 - i. 3 d.p.:

- 4 同 ト - 4 三 ト - 4

- a) 25.519
 - i. 1 d.p.: 25.5
 - ii. nearest unit: 26
 - iii. 2 d.p.: 25.52
- b) 321.0990
 - i. 3 d.p.: 321.099

- a) 25.519
 - i. 1 d.p.: 25.5
 - ii. nearest unit: 26
 - iii. 2 d.p.: 25.52
- b) 321.0990
 - i. 3 d.p.: 321.099
 - ii. nearest hundred:

- a) 25.519
 - i. 1 d.p.: 25.5
 - ii. nearest unit: 26
 - iii. 2 d.p.: 25.52
- b) 321.0990
 - i. 3 d.p.: 321.099
 - ii. nearest hundred: 300

- a) 25.519
 - i. 1 d.p.: 25.5
 - ii. nearest unit: 26
 - iii. 2 d.p.: 25.52
- b) 321.0990
 - i. 3 d.p.: 321.099
 - ii. nearest hundred: 300
 - iii. 2 d.p.:

- a) 25.519
 - i. 1 d.p.: 25.5
 - ii. nearest unit: 26
 - iii. 2 d.p.: 25.52
- b) 321.0990
 - i. 3 d.p.: 321.099
 - ii. nearest hundred: 300
 - iii. 2 d.p.: 321.10

- a) 25.519
 - i. 1 d.p.: 25.5
 - ii. nearest unit: 26
 - iii. 2 d.p.: 25.52
- b) 321.0990
 - i. 3 d.p.: 321.099
 - ii. nearest hundred: 300
 - iii. 2 d.p.: 321.10
- c) 54001.1

- a) 25.519
 - i. 1 d.p.: 25.5
 - ii. nearest unit: 26
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 - i. 3 d.p.: 321.099
 - ii. nearest hundred: 300
 - iii. 2 d.p.: 321.10
- c) 54001.1
 - i. nearest hundred:

- a) 25.519
 - i. 1 d.p.: 25.5
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- b) 321.0990
 - i. 3 d.p.: 321.099
 - ii. nearest hundred: 300
 - iii. 2 d.p.: 321.10
- c) 54001.1
 - i. nearest hundred: 54000

- a) 25.519
 - i. 1 d.p.: 25.5
 - ii. nearest unit: 26
 - iii. 2 d.p.: 25.52
- b) 321.0990
 - i. 3 d.p.: 321.099
 - ii. nearest hundred: 300
 - iii. 2 d.p.: 321.10
- c) 54001.1
 - i. nearest hundred: 54000
 - ii. nearest ten:

- a) 25.519
 - i. 1 d.p.: 25.5
 - ii. nearest unit: 26
 - iii. 2 d.p.: 25.52
- b) 321.0990
 - i. 3 d.p.: 321.099
 - ii. nearest hundred: 300
 - iii. 2 d.p.: 321.10
- c) 54001.1
 - i. nearest hundred: 54000
 - ii. nearest ten: 54000

- a) 25.519
 - i. 1 d.p.: 25.5
 - ii. nearest unit: 26
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- b) 321.0990
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 - iii. 2 d.p.: 321.10
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 - i. nearest hundred: 54000
 - ii. nearest ten: 54000
 - iii. 2 d.p.:

- a) 25.519
 - i. 1 d.p.: 25.5
 - ii. nearest unit: 26
 - iii. 2 d.p.: 25.52
- b) 321.0990
 - i. 3 d.p.: 321.099
 - ii. nearest hundred: 300
 - iii. 2 d.p.: 321.10
- c) 54001.1
 - i. nearest hundred: 54000
 - ii. nearest ten: 54000
 - iii. 2 d.p.: 54001.10

- a) 25.519
 - i. 1 d.p.: 25.5
 - ii. nearest unit: 26
 - iii. 2 d.p.: 25.52
- b) 321.0990
 - i. 3 d.p.: 321.099
 - ii. nearest hundred: 300
 - iii. 2 d.p.: 321.10
- c) 54001.1
 - i. nearest hundred: 54000
 - ii. nearest ten: 54000
 - iii. 2 d.p.: 54001.10

It is very important to realize the difference between the following numbers 1625.00, 1625.0 and 1625.

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If an answer to certain problem is given as 1625.00, it means that the answer is accurate to 2 d.p., so the actual answer can be any number x, such that 1624.995 $\leq x < 1625.005$.

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If an answer to certain problem is given as 1625.00, it means that the answer is accurate to 2 d.p., so the actual answer can be any number x, such that 1624.995 $\leq x < 1625.005$.

If however the answer is given as 1625, then this is correct to the nearest unit, so the actual number can be any number x, such that $1624.5 \le x < 1625.5$.

Rounding - decimal places

What's the conclusion of all this?

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Of course 444.60 = 444.6, but the rounded answer 444.60 indicates that the actual answer was between 444.595 and 444.605,

What's the conclusion of all this? If you were to round 444.5971 to 2 d.p. then the answer is 444.60 and **not** 444.6. The 0 at the end is important because it indicates the accuracy of the rounding.

Of course 444.60 = 444.6, but the rounded answer 444.60 indicates that the actual answer was between 444.595 and 444.605, while the rounded answer 444.6 indicates only that the actual answer was between 444.55 and 444.65.

We count significant figures starting from the first non-zero digit from the left and then count **every** digit (including the zeros).

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We count significant figures starting from the first non-zero digit from the left and then count **every** digit (including the zeros). Consider the number 0.004500545. The first non-zero digit from the left is 4, so this is our 1st significant figure, 5 is the second significant figure, 0 is the third, the next 0 is the fourth and so on. We will round the number to

1 s.f.: 0.005

- 1 s.f.: 0.005
- 2 s.f.: 0.0045

- 1 s.f.: 0.005 2 s.f.: 0.0045
- 3 s.f.: 0.00450

- 1 s.f.: 0.005 2 s.f.: 0.0045 3 s.f.: 0.00450
- 4 s.f.: 0.004501

- 1 s.f.: 0.005 2 s.f.: 0.0045 3 s.f.: 0.00450
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We count significant figures starting from the first non-zero digit from the left and then count **every** digit (including the zeros). Consider the number 0.004500545. The first non-zero digit from the left is 4, so this is our 1st significant figure, 5 is the second significant figure, 0 is the third, the next 0 is the fourth and so on. We will round the number to

- 1 s.f.: 0.005
- 2 s.f.: 0.0045
- 3 s.f.: 0.00450
- 4 s.f.: 0.004501

Now consider the number 918273.222, here 9 is the first significant figure, 1 is the second and so on.

We count significant figures starting from the first non-zero digit from the left and then count **every** digit (including the zeros). Consider the number 0.004500545. The first non-zero digit from the left is 4, so this is our 1st significant figure, 5 is the second significant figure, 0 is the third, the next 0 is the fourth and so on. We will round the number to

- 1 s.f.: 0.005
- 2 s.f.: 0.0045
- 3 s.f.: 0.00450
- 4 s.f.: 0.004501

Now consider the number 918273.222, here 9 is the first significant figure, 1 is the second and so on.We will round it to 4 s.f.: 918300

We count significant figures starting from the first non-zero digit from the left and then count **every** digit (including the zeros). Consider the number 0.004500545. The first non-zero digit from the left is 4, so this is our 1st significant figure, 5 is the second significant figure, 0 is the third, the next 0 is the fourth and so on. We will round the number to

- 1 s.f.: 0.005
- 2 s.f.: 0.0045
- 3 s.f.: 0.00450
- 4 s.f.: 0.004501

Now consider the number 918273.222, here 9 is the first significant figure,

 $1 \mbox{ is the second and so on.} We will round it to$

- 4 s.f.: 918300
- 3 s.f.: 918000

We count significant figures starting from the first non-zero digit from the left and then count **every** digit (including the zeros). Consider the number 0.004500545. The first non-zero digit from the left is 4, so this is our 1st significant figure, 5 is the second significant figure, 0 is the third, the next 0 is the fourth and so on. We will round the number to

- 1 s.f.: 0.005
- 2 s.f.: 0.0045
- 3 s.f.: 0.00450
- 4 s.f.: 0.004501

Now consider the number 918273.222, here 9 is the first significant figure,

 $1 \mbox{ is the second and so on.} We will round it to$

- 4 s.f.: 918300
- 3 s.f.: 918000
- 2 s.f.: 920000

We count significant figures starting from the first non-zero digit from the left and then count **every** digit (including the zeros). Consider the number 0.004500545. The first non-zero digit from the left is 4, so this is our 1st significant figure, 5 is the second significant figure, 0 is the third, the next 0 is the fourth and so on. We will round the number to

- 1 s.f.: 0.005
- 2 s.f.: 0.0045
- 3 s.f.: 0.00450
- 4 s.f.: 0.004501

Now consider the number 918273.222, here 9 is the first significant figure,

 $1 \mbox{ is the second and so on.} We will round it to$

- 4 s.f.: 918300
- 3 s.f.: 918000
- 2 s.f.: 920000
- 1 s.f.: 900000

a) 25.519

- a) 25.519
 - i. 1 s.f.:

- a) 25.519
 - i. 1 s.f.: 30

- a) 25.519 i. 1 s.f.: 30
 - ii. 2 s.f.:

- a) 25.519
 - i. 1 s.f.: 30
 - ii. 2 s.f.: 26

a) 25.519 i. 1 s.f.: 30 ii. 2 s.f.: 26 iii. 3 s.f.:

- a) 25.519 i. 1 s.f.: 30 ii. 2 s.f.: 26
 - iii. 3 s.f.: 25.5

a) 25.519

1 s.f.: 30
2 s.f.: 26
3 s.f.: 25.5

b) 321.0990

a) 25.519

1 s.f.: 30
2 s.f.: 26
3 s.f.: 25.5

b) 321.0990

3 s.f.:

a) 25.519

1 s.f.: 30
2 s.f.: 26
3 s.f.: 25.5

b) 321.0990

3 s.f.: 321

a) 25.519

1 s.f.: 30
2 s.f.: 26
3 s.f.: 25.5

b) 321.0990

3 s.f.: 321
4 s.f.:

a) 25.519

1 s.f.: 30
2 s.f.: 26
3 s.f.: 25.5

b) 321.0990

3 s.f.: 321
4 s.f.: 321.1

a) 25.519

1 s.f.: 30
2 s.f.: 26
3 s.f.: 25.5

b) 321.0990

3 s.f.: 321
4 s.f.: 321.1
5 s.f.:

a) 25.519

1 s.f.: 30
2 s.f.: 26
3 s.f.: 25.5

b) 321.0990

3 s.f.: 321
4 s.f.: 321.1
5 s.f.: 321.10

- 4 同 ト - 4 三 ト - 4

- a) 25.519

 1 s.f.: 30
 2 s.f.: 26
 3 s.f.: 25.5

 b) 321.0990

 3 s.f.: 321
 4 s.f.: 321.1
 5 s.f.: 321.10
- c) 0.002999

- a) 25.519

 1 s.f.: 30
 2 s.f.: 26
 3 s.f.: 25.5

 b) 321.0990

 3 s.f.: 321
 4 s.f.: 321.1
 5 s.f.: 321.10

 c) 0.002999
 - i. 1 s.f.:

- a) 25.519

 1 s.f.: 30
 2 s.f.: 26
 3 s.f.: 25.5

 b) 321.0990

 3 s.f.: 321
 4 s.f.: 321.1
 5 s.f.: 321.10

 c) 0.002999
 - i. 1 s.f.: 0.003

- a) 25.519

 1 s.f.: 30
 2 s.f.: 26
 3 s.f.: 25.5

 b) 321.0990

 3 s.f.: 321
 4 s.f.: 321.1
 5 s.f.: 321.10

 c) 0.002999

 1 s.f.: 0.003
 - i. 1 s.i.. 0.

- a) 25.519

 1 s.f.: 30
 2 s.f.: 26
 3 s.f.: 25.5

 b) 321.0990

 3 s.f.: 321
 4 s.f.: 321.1
 5 s.f.: 321.10

 c) 0.002999

 1 s.f.: 0.003
 - ii. 2 s.f.: 0.0030

- a) 25.519 i. 1 s.f.: 30 ii. 2 s.f.: 26 iii. 3 s.f.: 25.5 b) 321.0990 i 3 s.f.: 321 ii 4 s.f.: 321.1 iii. 5 s.f.: 321.10 c) 0.002999 i. 1 s.f.: 0.003 ii. 2 s.f.: 0.0030
 - iii. 3 s.f.:

- a) 25.519 i. 1 s.f.: 30 ii. 2 s.f.: 26 iii. 3 s.f.: 25.5 b) 321.0990 i 3 s.f.: 321 ii 4 s.f.: 321.1 iii. 5 s.f.: 321.10 c) 0.002999 i. 1 s.f.: 0.003 ii. 2 s.f.: 0.0030
 - iii. 3 s.f.: 0.00300

- a) 25.519 i. 1 s.f.: 30 ii. 2 s.f.: 26 iii. 3 s.f.: 25.5 b) 321.0990 i 3 s.f.: 321 ii 4 s.f.: 321.1 iii. 5 s.f.: 321.10 c) 0.002999 i. 1 s.f.: 0.003 ii. 2 s.f.: 0.0030
 - iii. 3 s.f.: 0.00300

Again we need to remember that there is a difference between the answer 300 correct to 1 s.f. and 300 correct to 2 s.f. etc.

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If the answer given is 300 correct to 1 s.f., then the actual answer could have been any number between 250 and 350,

Again we need to remember that there is a difference between the answer 300 correct to 1 s.f. and 300 correct to 2 s.f. etc.

If the answer given is 300 correct to 1 s.f., then the actual answer could have been any number between 250 and 350, and if the answer given is 300 correct to 2 s.f., then the actual answer could have been any number between 295 and 305.

Standard form

A number is written in a standard form if it's in the form $a \times 10^k$, where $1 \le a < 10$ and $k \in \mathbb{Z}$

Note the term **standard form** is used in UK, while the term **scientific notation** is used in US. Both mean the same thing. We will use 'standard form', but you should know both.

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Consider the following list of numbers:

12112, 0.453, 9, 0.56 $\times \, 10^3,$ 353 $\times \, 10^{-5}$

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Consider the following list of numbers:

 $12112, \qquad 0.453, \qquad 9, \qquad 0.56\times 10^3, \qquad 353\times 10^{-5}$ How many of these numbers are written in standard form?

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Consider the following list of numbers:

 $12112, \qquad 0.453, \qquad 9, \qquad 0.56\times 10^3, \qquad 353\times 10^{-5}$ How many of these numbers are written in standard form? None.

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12112, 0.453, 9, 0.56×10^3 , 353×10^{-5} How many of these numbers are written in standard form? None. The first three are missing the 10^k part, for the last two *a* is not between 1 and 10.

Note the term **standard form** is used in UK, while the term **scientific notation** is used in US. Both mean the same thing. We will use 'standard form', but you should know both.

Consider the following list of numbers:

12112, 0.453, 9, 0.56×10^3 , 353×10^{-5} How many of these numbers are written in standard form? None. The first three are missing the 10^k part, for the last two *a* is not between 1 and 10. We can turn them all into the standard form:

$$1.2112 \times 10^4, \qquad 4.53 \times 10^{-1}, \qquad 9 \times 10^0, \qquad 5.6 \times 10^2, \qquad 3.53 \times 10^{-3} \times 10^{-3$$

Write the following numbers in the standard form: $123 = 1.23 \times 10^2 \text{,} \label{eq:constraint}$

Write the following numbers in the standard form: $123 = 1.23 \times 10^2 \text{,} \\ 20030$

 $123 = 1.23 \times 10^2$, $20030 = 2.003 \times 10^4$,

Image: A matrix and A matrix

 $\begin{array}{l} 123 = 1.23 \times 10^2,\\ 20030 = 2.003 \times 10^4,\\ 0.4561 \end{array}$

Image: A matrix and A matrix

$$\begin{split} 123 &= 1.23 \times 10^2 \text{,} \\ 20030 &= 2.003 \times 10^4 \text{,} \\ 0.4561 &= 4.561 \times 10^{-1} \text{,} \end{split}$$

$$\begin{split} 123 &= 1.23 \times 10^2, \\ 20030 &= 2.003 \times 10^4, \\ 0.4561 &= 4.561 \times 10^{-1}, \\ 2 \end{split}$$

$$\begin{split} 123 &= 1.23 \times 10^2, \\ 20030 &= 2.003 \times 10^4, \\ 0.4561 &= 4.561 \times 10^{-1}, \\ 2 &= 2 \times 10^0, \end{split}$$

```
\begin{split} 123 &= 1.23 \times 10^2, \\ 20030 &= 2.003 \times 10^4, \\ 0.4561 &= 4.561 \times 10^{-1}, \\ 2 &= 2 \times 10^0, \\ 0.000023 \end{split}
```

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\begin{split} 123 &= 1.23 \times 10^2,\\ 20030 &= 2.003 \times 10^4,\\ 0.4561 &= 4.561 \times 10^{-1},\\ 2 &= 2 \times 10^0,\\ 0.000023 &= 2.3 \times 10^{-5},\\ 10 \end{split}
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If you have any questions or doubts email me at T.J.Lechowski@gmail.com